

Multilabel Prediction of Drug Activity¹

Hongyu Su, Markus Heinonen, Juho Rousu



Department of Computer Science
University of Helsinki

Machine Learning in Systems Biology, Edinburgh
October 16, 2010

¹Su et al: Structured Output Prediction of Anti-Cancer Drug Activity. Pattern Recognition in Bioinformatics. Lecture Notes in Computer Science, 2010, Volume 6282, 38–49

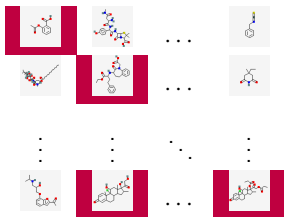
Drug bioactivity classification

- Given molecule, predict active/not active
- State of the art method: SVM with graph kernels over the molecules



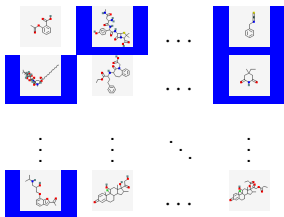
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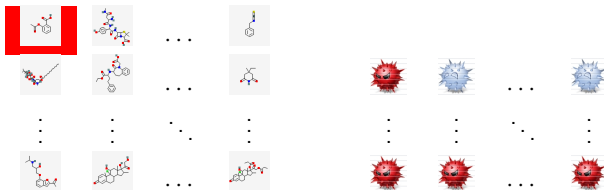
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Predicting activity against multiple targets

- There are numerous targets (different viruses, cancer types, ...) that share characteristics
- Can we predict the activity better by learning against all available targets at the same time?



Multilabel classification

- Single label classification :

$$x_i \xrightarrow{\text{predict}} y_i, y_i \in \{0, 1\}$$

- **Multilabel classification:** Multiple labels (targets) associate with each example.

$$x_i \xrightarrow{\text{predict}} \mathbf{y}_i = y_1 \times y_2 \times \cdots \times y_k, y_i \in \{0, 1\}$$

- **Basic approach:** Build a single-label classifier for each individual label, compose the multilabels from their output
 - Does not benefit from possible statistical dependencies between labels
- **Structured output prediction:** utilize structure (graph, tree, sequence) of the output to predict the multilabel in a single shot
 - Leverage on the correlation of neighboring labels

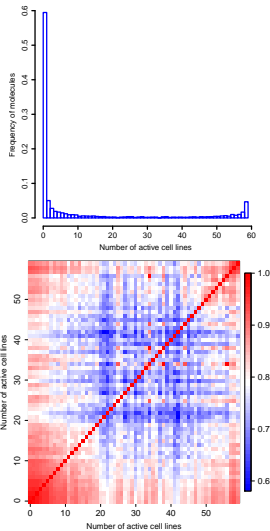
Method: Max-Margin Conditional Random Field (MMCRF)

- Method originally proposed in Rousu, Saunders, Szedmak, Shawe-Taylor. Efficient algorithms for max-margin structured classification. In *Predicting Structured Data*, MIT Press, 2007, pp. 105–129
- Relative of M^3N (Taskar et al. 2003) - but assumes fixed output structure, different optimization algorithm
- Generalization of the hierarchical multilabel classifier HM^3 (Rousu et al. 2005;2006) to fixed general graphs.
- Based on Conditional Random Field model over a network of outputs:

$$P(\mathbf{y}|x) \propto \prod_{e \in \mathcal{E}} \exp(\mathbf{w}_e^T \varphi_e(x, \mathbf{y}_e)),$$

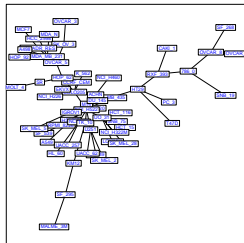
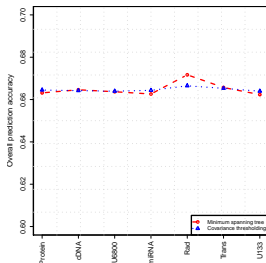
NCI-cancer Dataset

- NCI-cancer dataset contains > 4000 molecules with anti-cancer activity against ~ 60 cancer celllines (cancer types).
- **Histogram** shows the distribution of molecules according to the activity.
 - Each bar contains molecules active against given number of targets
 - Skewed multilabel distribution
- **Heatmap** shows the similarity between pair of activity groups.
 - Inactive molecules are mutually similar
 - So are molecules that are active against all targets
 - And the extremes are similar to each other



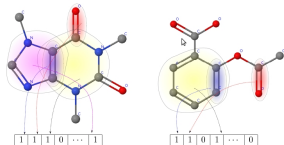
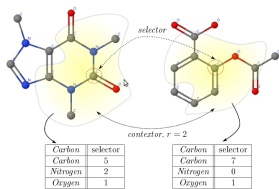
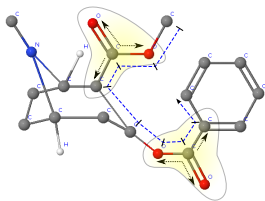
Output representation: embedding of a labeled network

- No pre-existing structure between the drug targets, but lots of microarray data on the cell lines them selves:
Reverse-phase lysate, cDNA, Affymetric HU6800, miRNA, ABC transporter Radiation RNA array
- Each gives a correlation matrix between the cell lines (how similarly the cell lines respond)
- Extract network from the correlation matrix: Maximum weighted spanning tree, Correlation thresholding, ...
- Multilabel \mathbf{y} induces a labeling of the network
- Embed the (labelled) network to a feature space: $\psi_{e,u}(\mathbf{y}) = 1$ iff in multilabel \mathbf{y} edge e is labeled u , $u \in \{00,01,10,11\}$



Input representation: Kernels over molecular graphs

- Various kernels applicable for molecular graphs, and have previously been used in single-label molecular classification tasks
 - Walk kernels (top picture): count matching walks (e.g. C-O-C-C-C-O-C-C-C) in two molecular graphs
 - Weighted decomposition kernel (middle): matches neighbourhoods of same-labeled nodes in two molecular graphs
 - Tanimoto kernel (bottom): kernel over user-defined salient substructures (molecular fingerprints)
- Tanimoto works the best

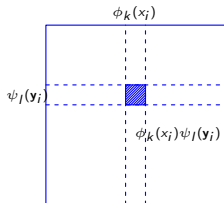


Joint feature map $\varphi(x, \mathbf{y})$

- Learning happens in feature space joint for inputs and outputs
- The feature map contains products of all input (molecule graph) and output feature (edge-labeling) pairs via the tensor (outer) product:

$$\varphi(x, \mathbf{y}) = \phi(x) \otimes \psi(\mathbf{y})$$

- The formulation lets us learn context (edge-labeling) specific feature weights for a global set of input features
 - No assumption of alignment between input and output features

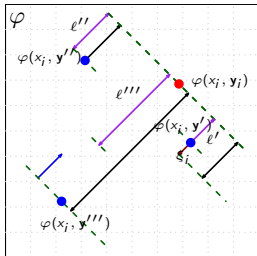


Learning MMCRF: overview

The MMCRF framework consists of the following components

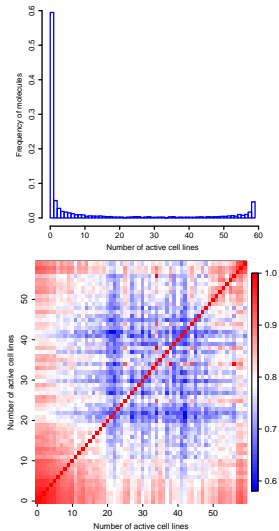
- Max-margin learning: Maximize the margin between real example $\varphi(x_i, \mathbf{y}_i)$ and all the incorrect pseudo-examples $\varphi(x_i, \mathbf{y})$, whilst controlling the norm of the weight vector
- Use of kernels $K(x, x')$ to tackle high-dimensionality of input feature maps
- Use of graphical model techniques for tackle the exponential size of the multilabel space

$$\begin{aligned} \min_{\mathbf{w}, \xi \geq 0} & \left(\frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^n \xi_i \right) \\ \text{s.t. } & \mathbf{w}^T \phi(x_i, \mathbf{y}_i) - \mathbf{w}^T \phi(x_i, \mathbf{y}) \\ & \geq \ell_{\Delta}(\mathbf{y}_i, \mathbf{y}) - \xi_i, \forall x_i, \mathbf{y}. \end{aligned}$$



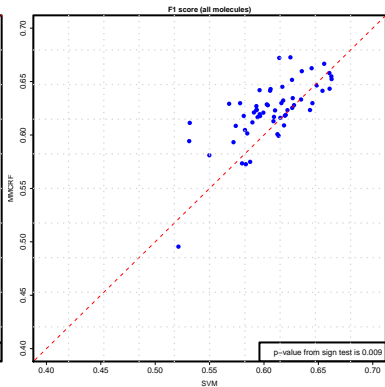
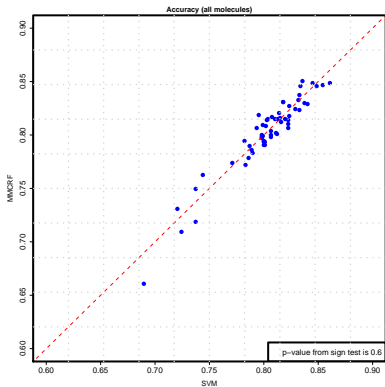
Data preprocessing

- Three versions of the dataset prepared
 - Full data.
 - With no zero active molecules (group 0 removed).
 - With middle-active molecules (groups 0-10 and 50-59 removed)
- 5-fold stratified cross-validation used:
 - divide each activity group into 5-folds
 - merge across groups to create global folds
 - ensures that each group is represented in each fold



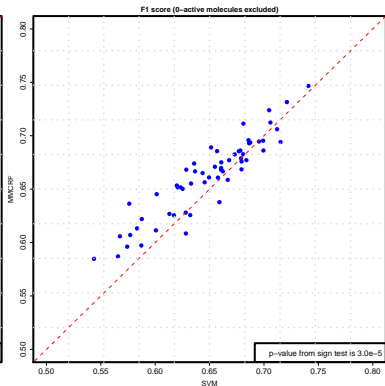
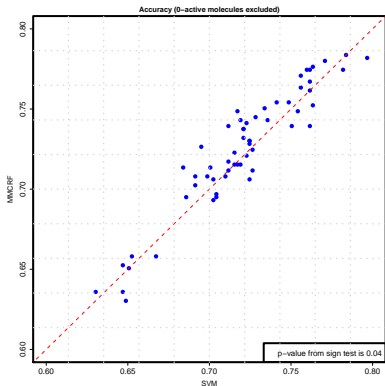
Prediction Accuracy/F1: Full Data

- The scatter plots show prediction accuracy (left) and F1 (right) of MMCRF (y-axis) against SVM (x-axis) for each cell line (blue dots)
- In terms of accuracy the two methods work equally well
- In terms of F1, MMCRF better than SVM



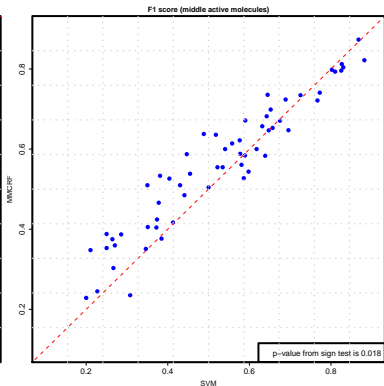
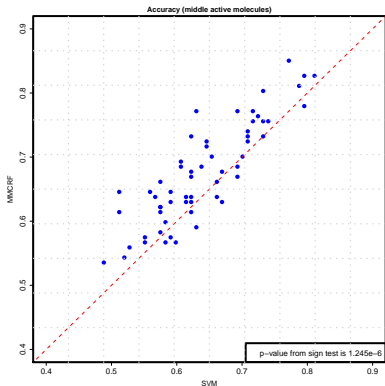
Prediction Accuracy/F1: Zero-actives removed

- The scatter plots show prediction accuracy (left) and F1 (right) of MMCRF (y-axis) against SVM (x-axis) for each cell line (blue dots)
- MMCRF significantly better in terms of accuracy and F1



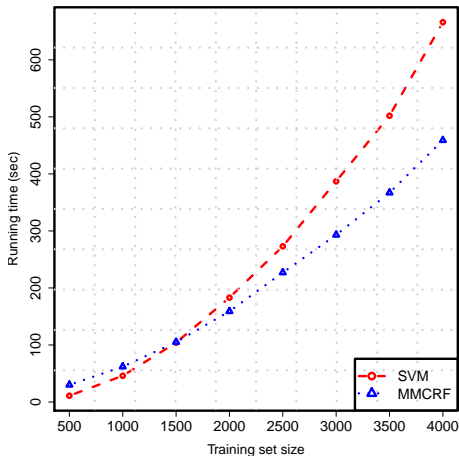
Prediction Accuracy/F1: Middle-actives only

- The scatter plots show prediction accuracy (left) and F1 (right) of MMCRF (y-axis) against SVM (x-axis) for each cell line (blue dots)
- MMCRF significantly better in terms of accuracy and F1



Computation Time

- The plot shows the running time required for training MMCRF (1 multilabel model) and SVM (libsvm) (59 single label models).
- MMCRF (native Matlab code) scales better than libsvm (C++) on large datasets



Conclusions

- We proposed a structured output prediction approach for the classification of drug-like molecules.
- It is, to our knowledge, the first multilabel classification approach for the problem.
- The method is able to utilize the the statistical dependencies between multiple labels by means of a network constructed from auxiliary data available for the targets.
- In our experiments, the MMCRF outperforms the state-of-the-art SVM
- Future work includes
 - studying the effect of the output structure to predictive accuracy (learning algorithms, tree vs. general graph, other graph-theoretic properties)
 - better tackling of the skewness of the multilabel distribution
 - deeper look at cell line and drug molecule properties that explain good/bad performance