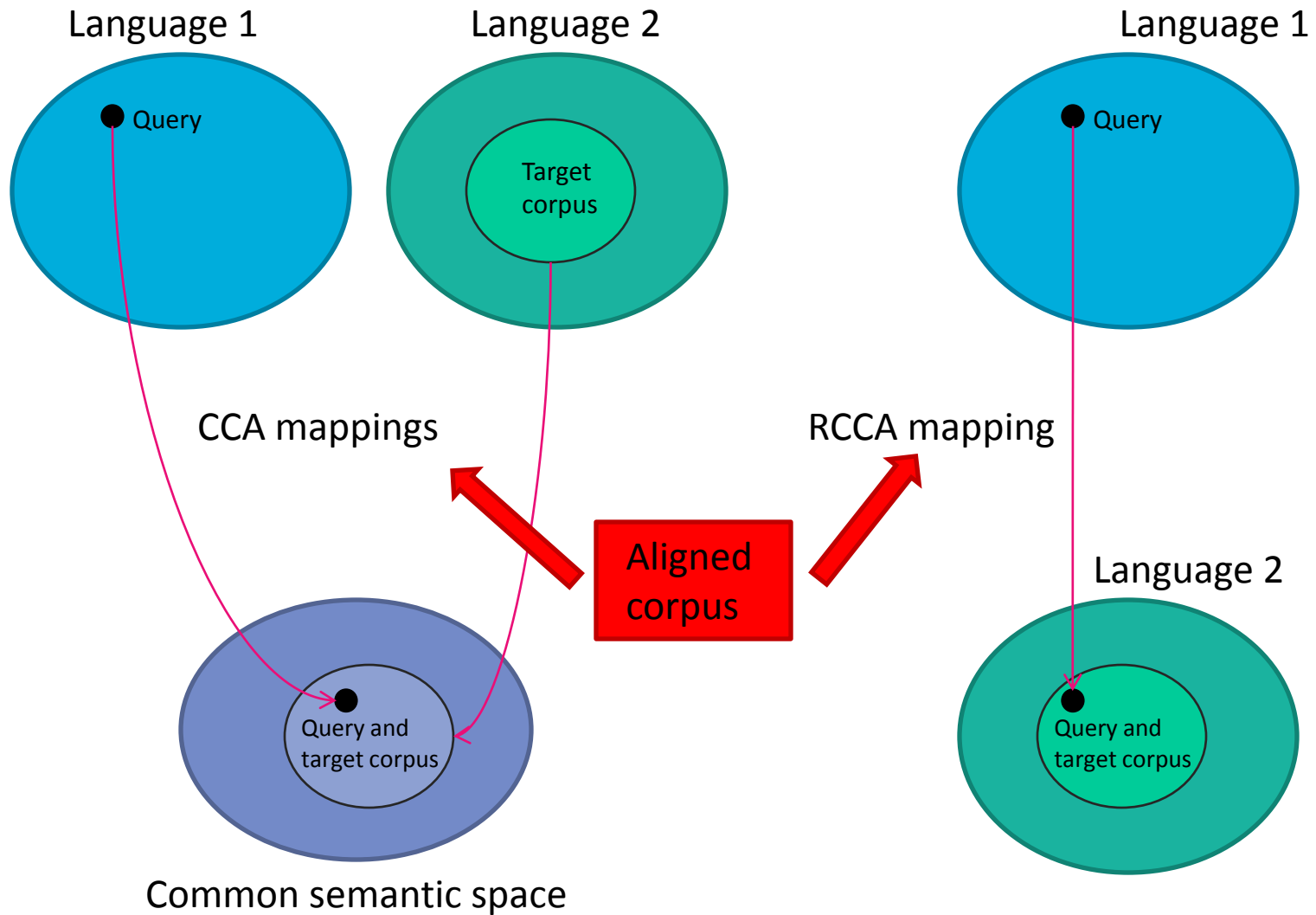


Regression CCA – information retrieval



Optimization problem

$\mathbf{X} \in \mathbb{R}^{m,d}$, $\mathbf{Y} \in \mathbb{R}^{n,d}$ (aligned corpus), $\mathbf{q} \in \mathbb{R}^m$ (query)

Optimization problem:

$$\begin{aligned} \max_{\alpha} \quad & \mathbf{q}'\mathbf{X}\mathbf{Y}'\alpha \\ \text{s.t.} \quad & \alpha'\mathbf{Q}\alpha = 1 \end{aligned}$$

- Regularized variance: $\mathbf{Q} := (1-\kappa)\mathbf{Y}\mathbf{Y}' + \kappa\mathbf{I}$
- Lagrangian \rightarrow system of linear equations.

Solution:

$$\alpha := \mathbf{Q}^{-1}(\mathbf{Y}\mathbf{X}'\mathbf{q}) \quad (\text{without rescaling})$$

Conjugate Gradient method suitable, take advantage of sparsity

Can be done online in query time!