

# Learning for Control from Multiple Demonstrations

Adam Coates, Pieter Abbeel, and Andrew Y. Ng  
Stanford University

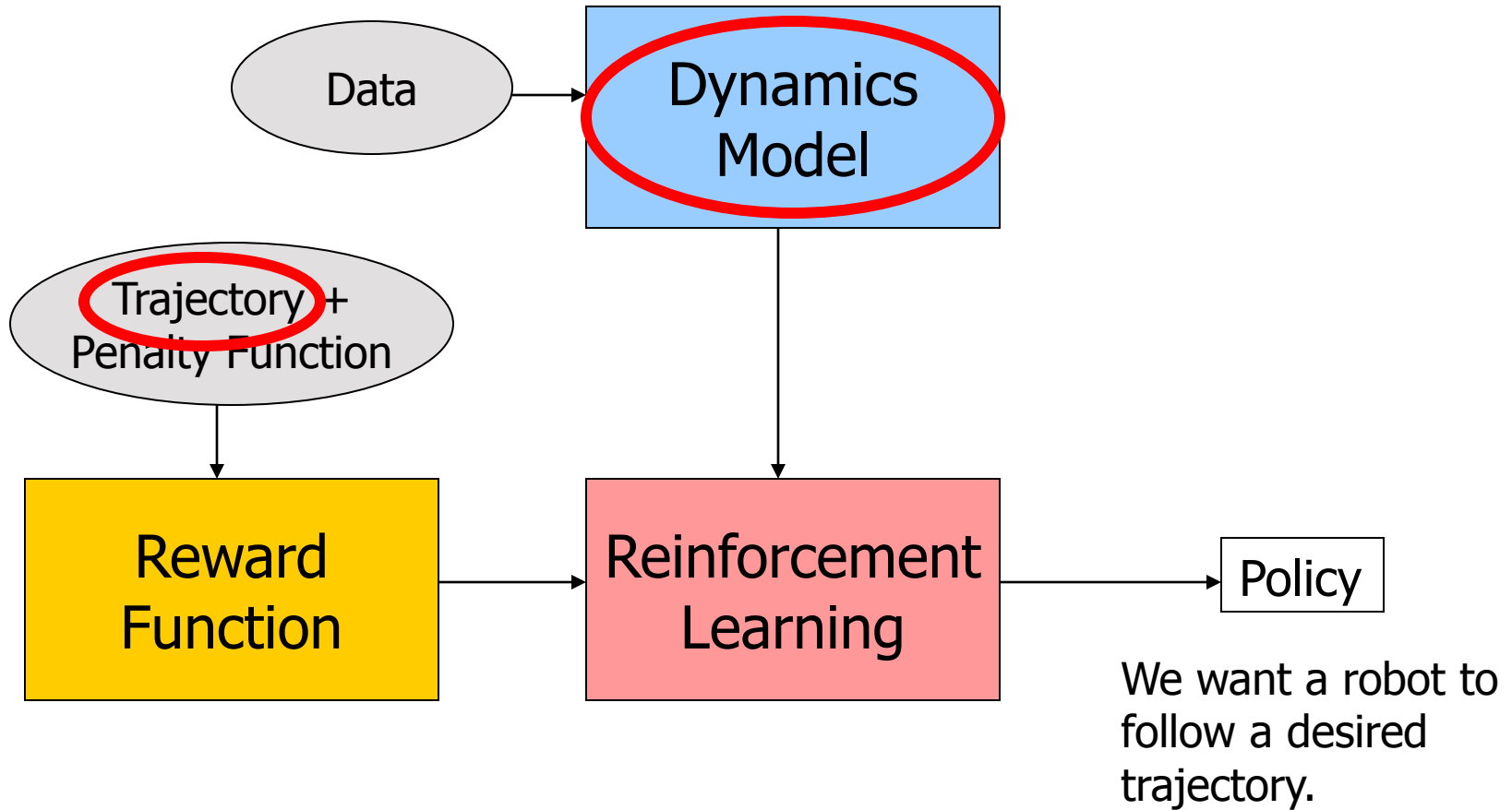
ICML 2008

# Motivating example



- How do we specify a task like this???

# Introduction



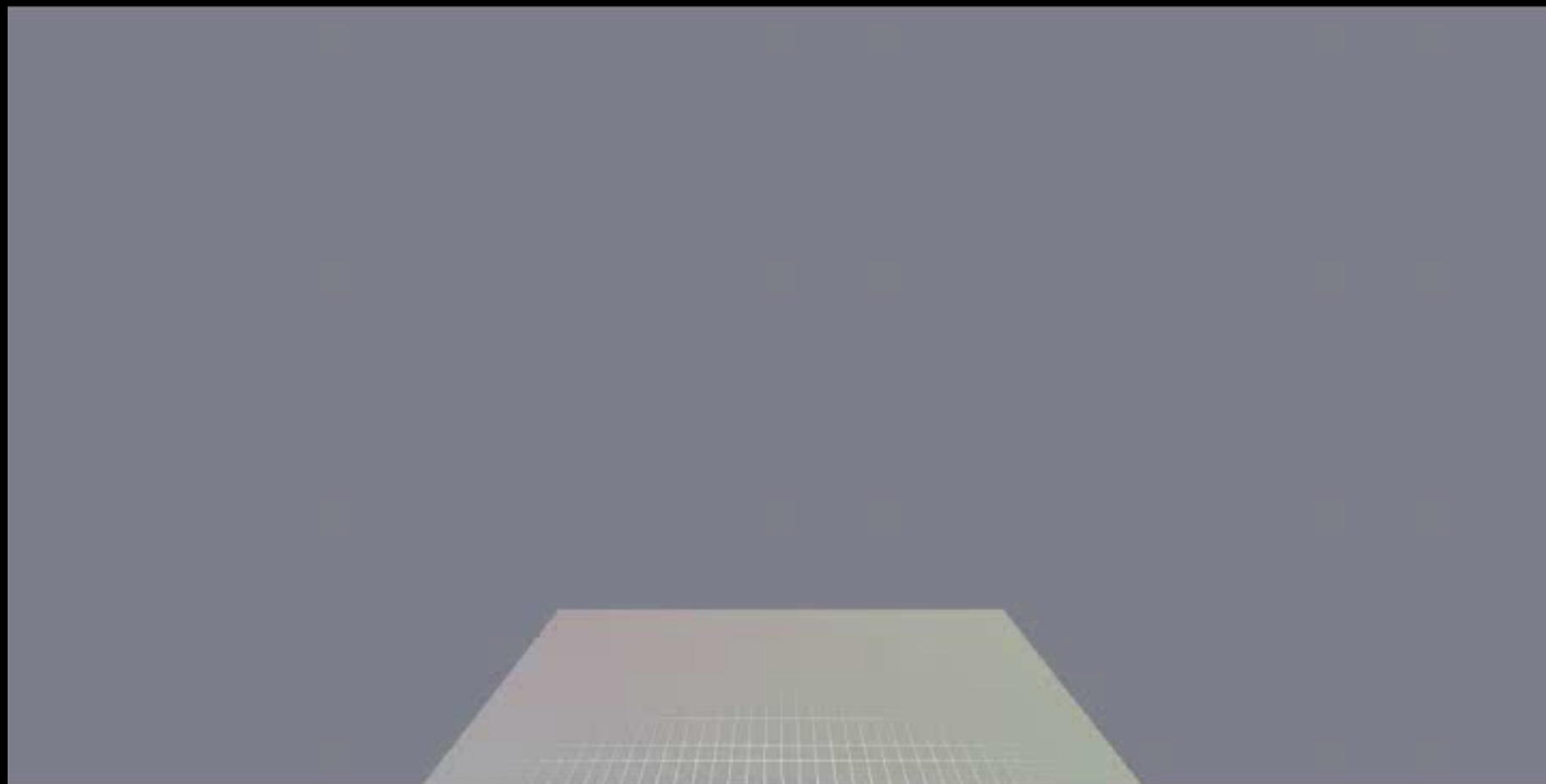
# Key difficulties

- Often very difficult to specify trajectory by hand.
  - Difficult to articulate exactly how a task is performed.
  - The trajectory should obey the system dynamics.
- ~~■ Use an expert *demonstration* as trajectory.
  - But, getting perfect demonstrations is hard.~~
- Use multiple suboptimal demonstrations.

# Outline

- Generative model for multiple suboptimal demonstrations.
- Learning algorithm that extracts:
  - Intended trajectory
  - High-accuracy dynamics model
- Experimental results:
  - Enabled us to fly autonomous helicopter aerobatics well beyond the capabilities of any other autonomous helicopter.

# Expert demonstrations: Airshow

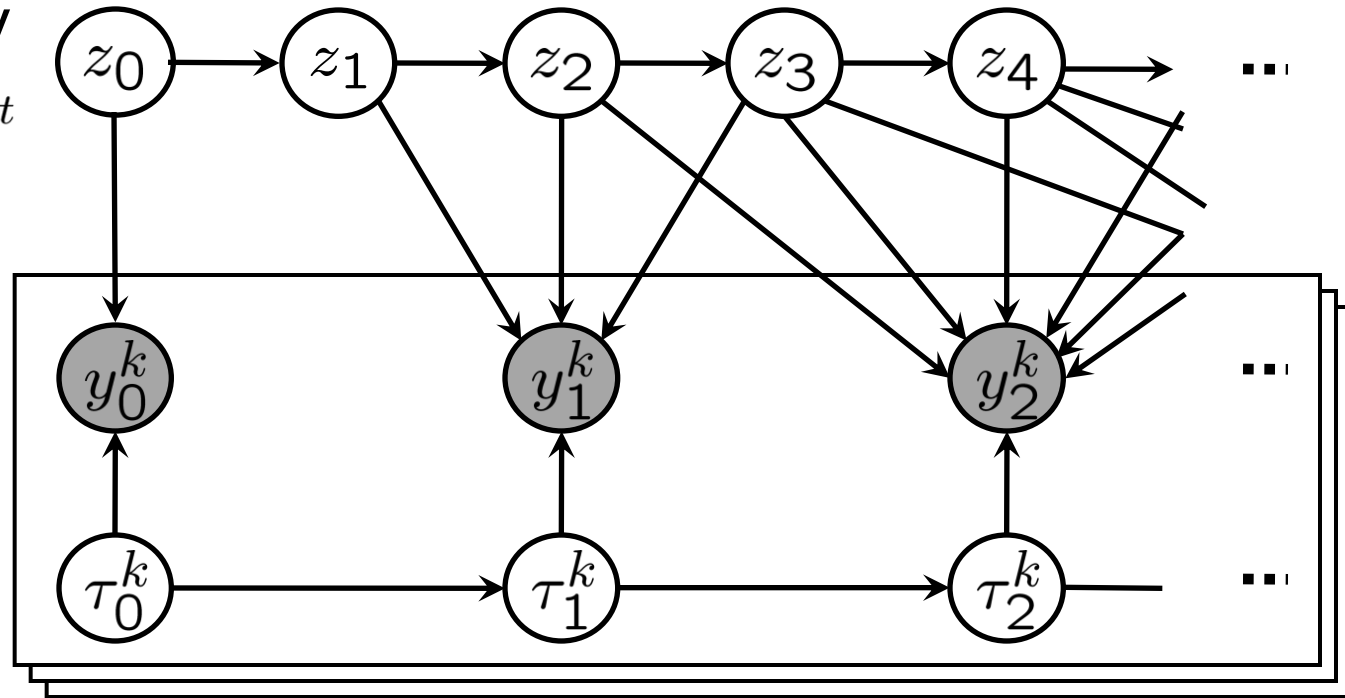


# Graphical model

Intended trajectory  
 $z_{t+1} = f(z_t) + \omega_t$

Expert  
demonstrations  
 $y_j = z_{\tau_j} + \nu_j$

Time indices



- Intended trajectory satisfies dynamics.
- Expert trajectory is a noisy observation of one of the hidden states.
  - But we don't know exactly which one.

# Learning algorithm

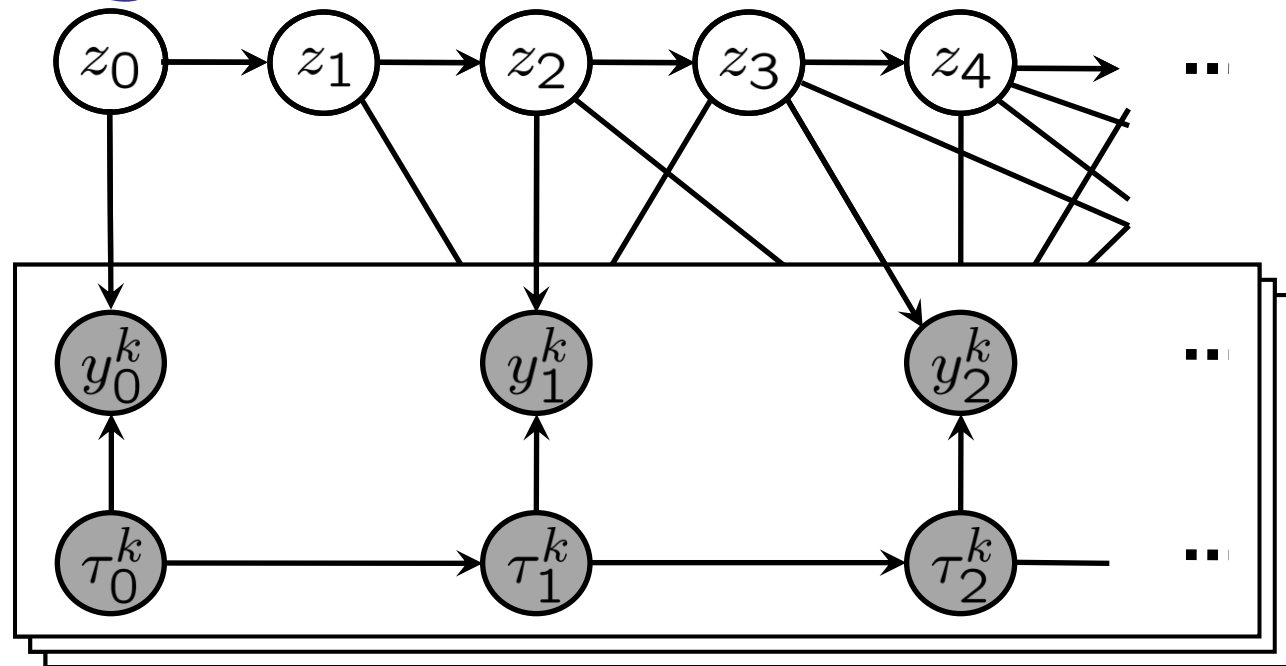
- Similar models appear in speech processing, genetic sequence alignment.
  - See, e.g., Listgarten et. al., 2005
- Maximize likelihood of the demonstration data over:
  - Intended trajectory states
  - Time index values
  - Variance parameters for noise terms
  - Time index distribution parameters



# Learning algorithm

If  $\tau$  is unknown,  
inference is hard.

If  $\tau$  is known, we  
have a standard  
HMM.



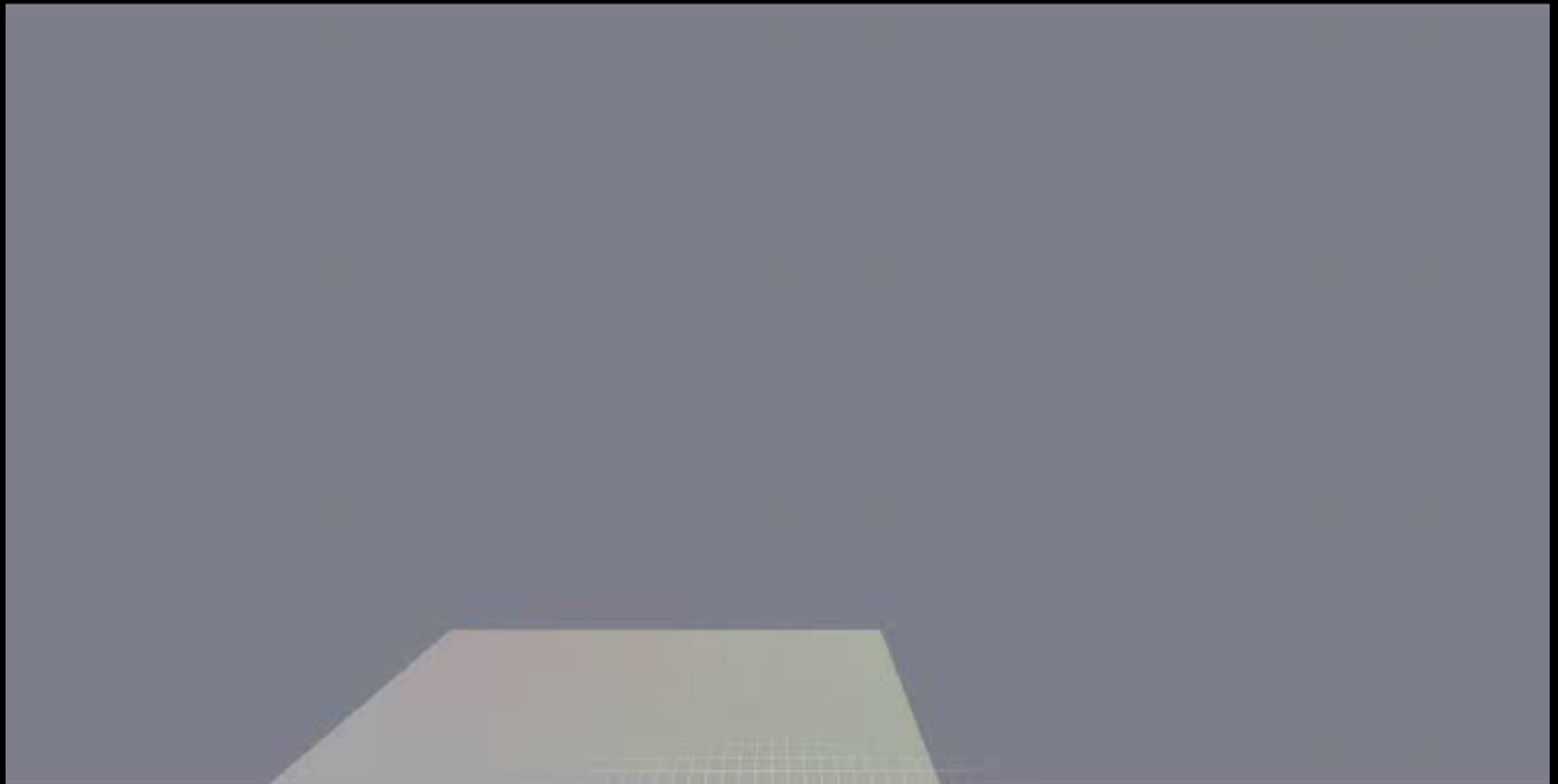
- Make an initial guess for  $\tau$ .
- Alternate between:
  - Fix  $\tau$ . Run EM on resulting HMM.
  - Choose new  $\tau$  using dynamic programming.

# Details: Incorporating prior knowledge

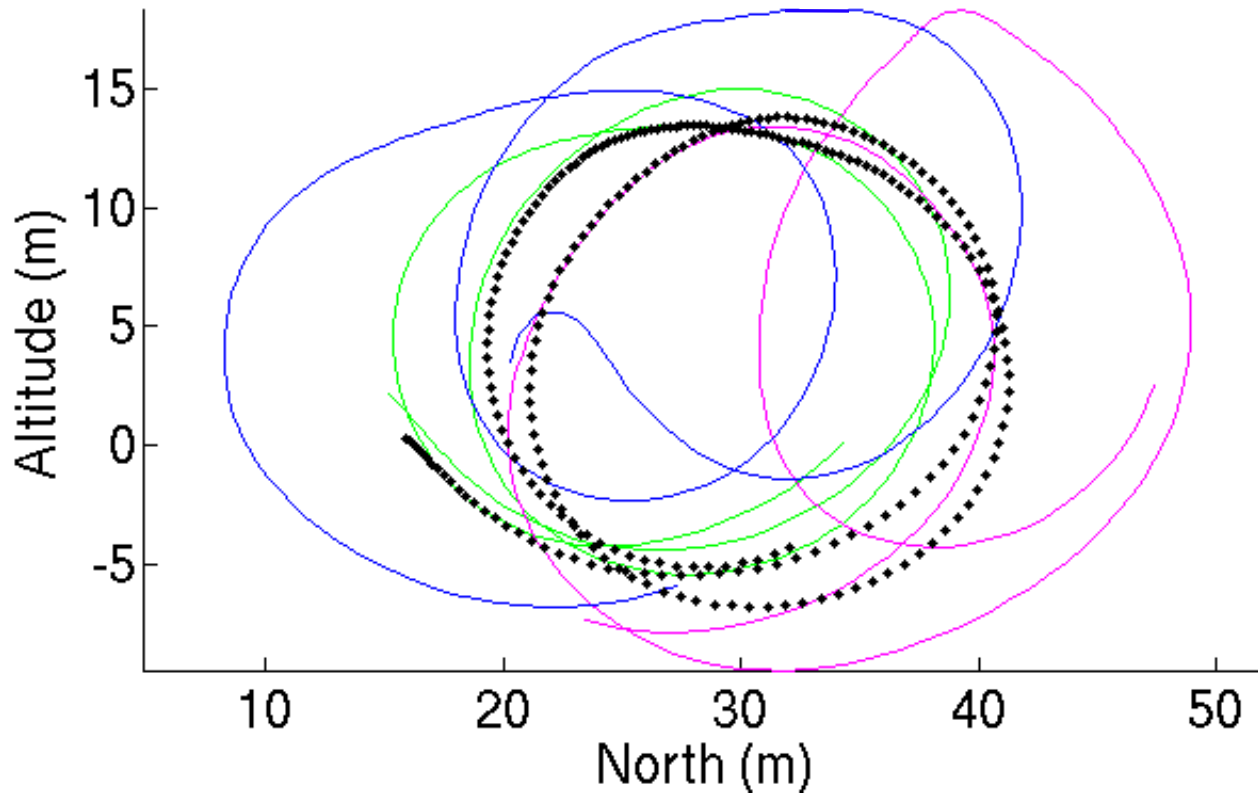
- Might have some limited knowledge about how the trajectory should look.
  - Flips and rolls should stay in place.
  - Vertical loops should lie in a vertical plane.
  - Pilot tends to “drift” away from intended trajectory.

# Results: Time-aligned demonstrations

- White helicopter is inferred “intended” trajectory.

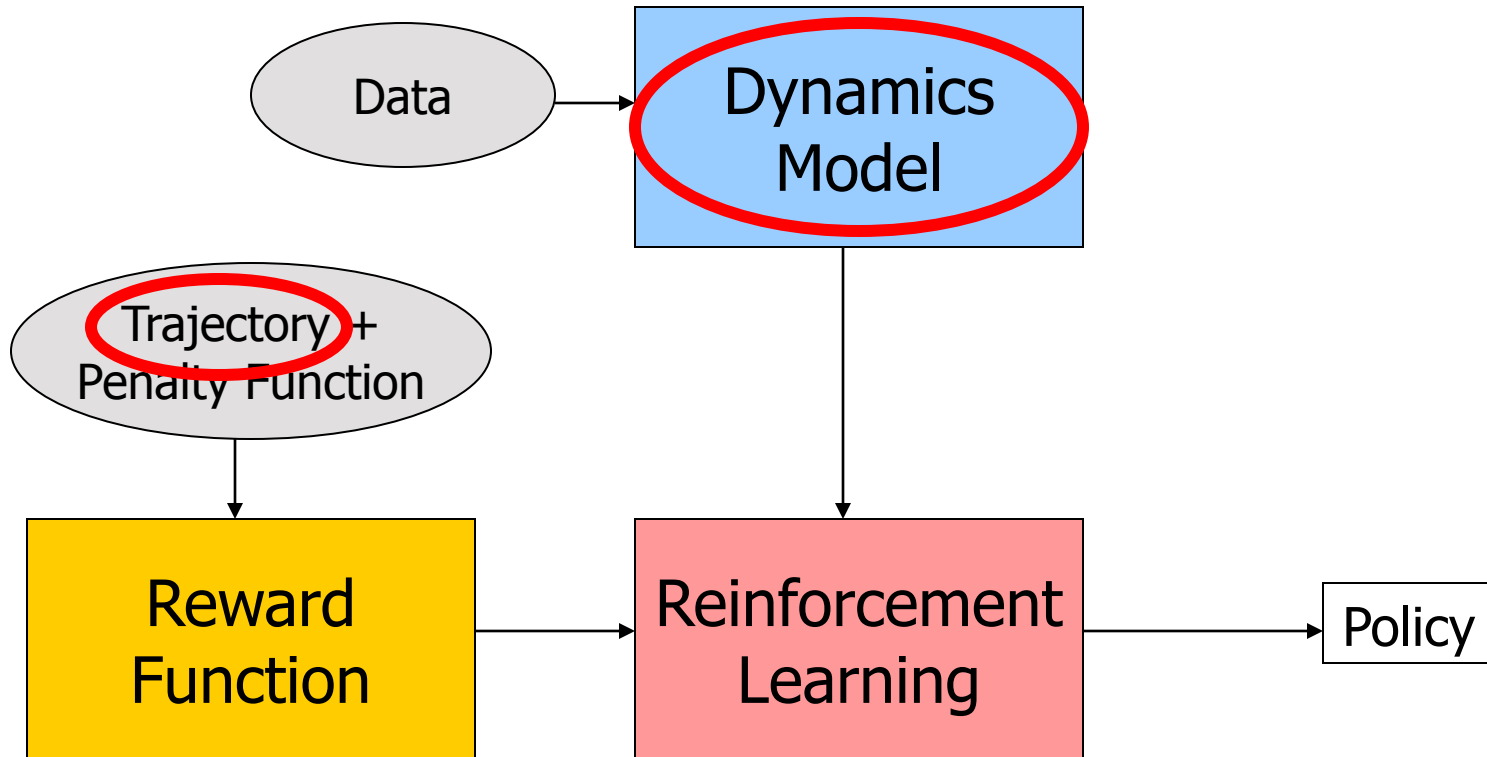


# Results: Loops



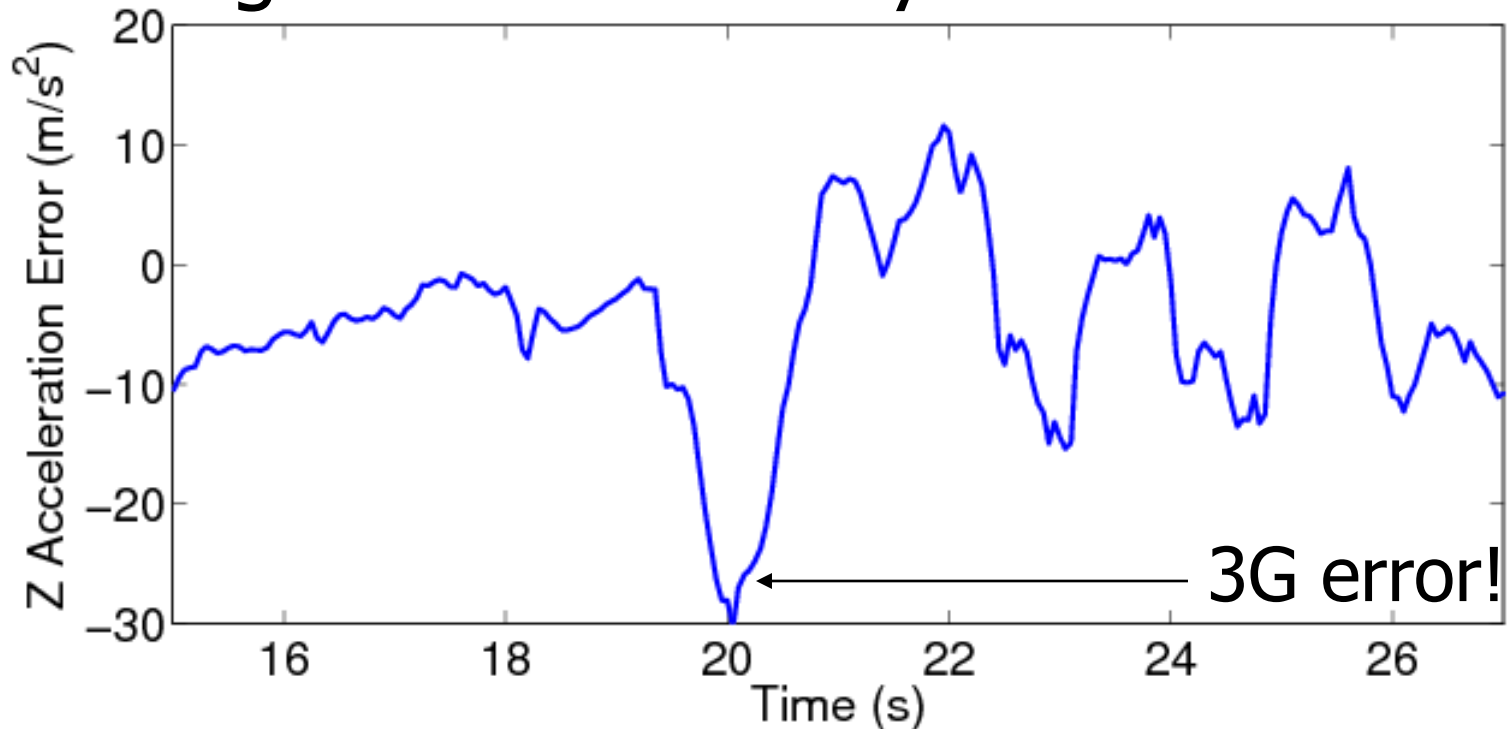
- Even without prior knowledge, the inferred trajectory is much closer to an ideal loop.

# Recap

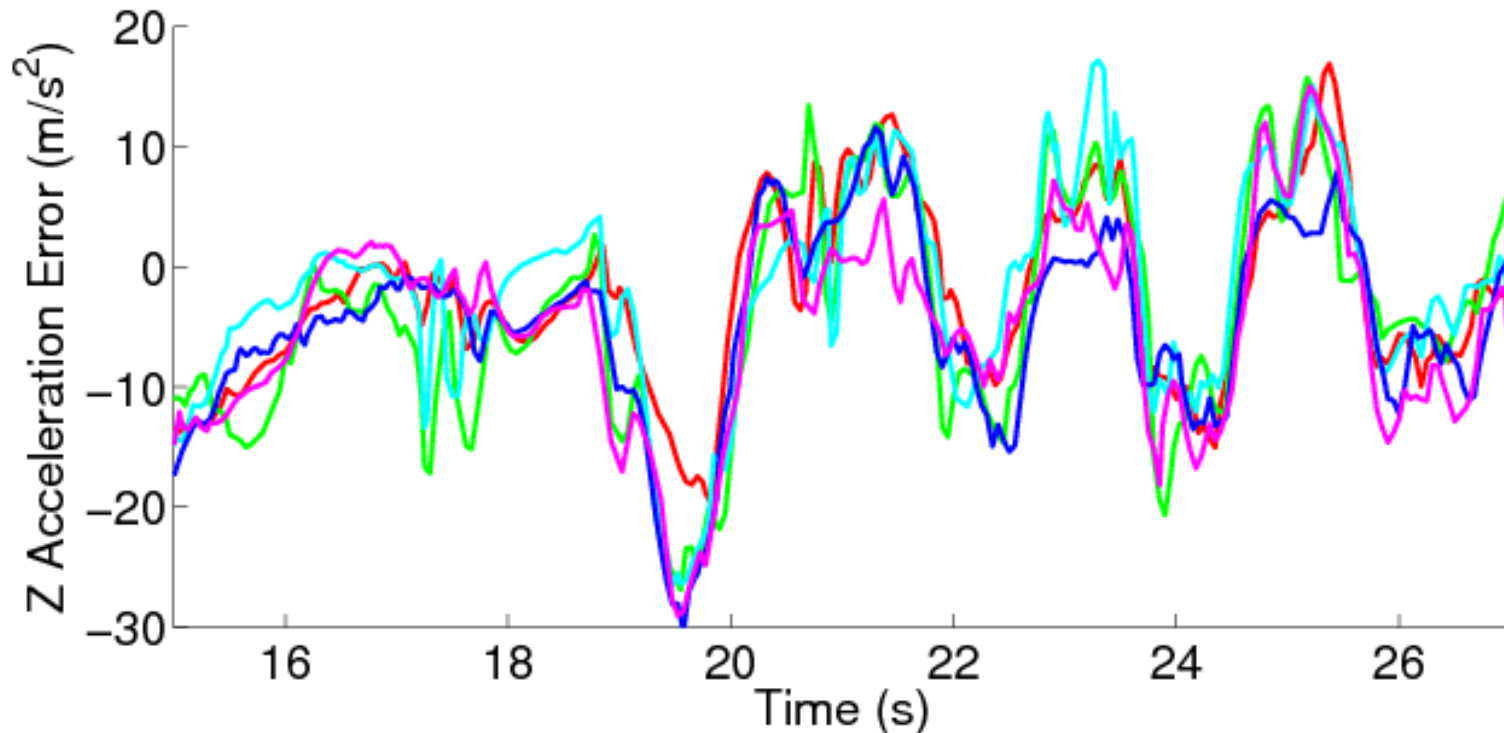


# Standard modeling approach

- Collect data
  - Pilot attempts to cover all flight regimes.
- Build global model of dynamics



# Errors aligned over time



- Errors observed in the “crude” model are clearly consistent after aligning demonstrations.

# Model improvement

- Key observation:

If we fly the same trajectory repeatedly, errors are consistent over time once we align the data.

- There are many hidden variables that we can't expect to model accurately.
  - Air (!), rotor speed, actuator delays, etc.
- If we fly the same trajectory repeatedly, the hidden variables tend to be the same each time.



# Trajectory-specific local models

- Learn locally-weighted model from aligned demonstration data.
  - Since data is aligned in time, we can weight by *time* to exploit repeatability of hidden variables.
  - For model at time  $t$ :  $W(t') = \exp(- (t - t')^2 / \sigma^2 )$
- Suggests an algorithm alternating between:
  - Learn trajectory from demonstration.
  - Build new models from aligned data.
- Can actually infer an improved model *jointly* during trajectory learning.

# Experiment setup

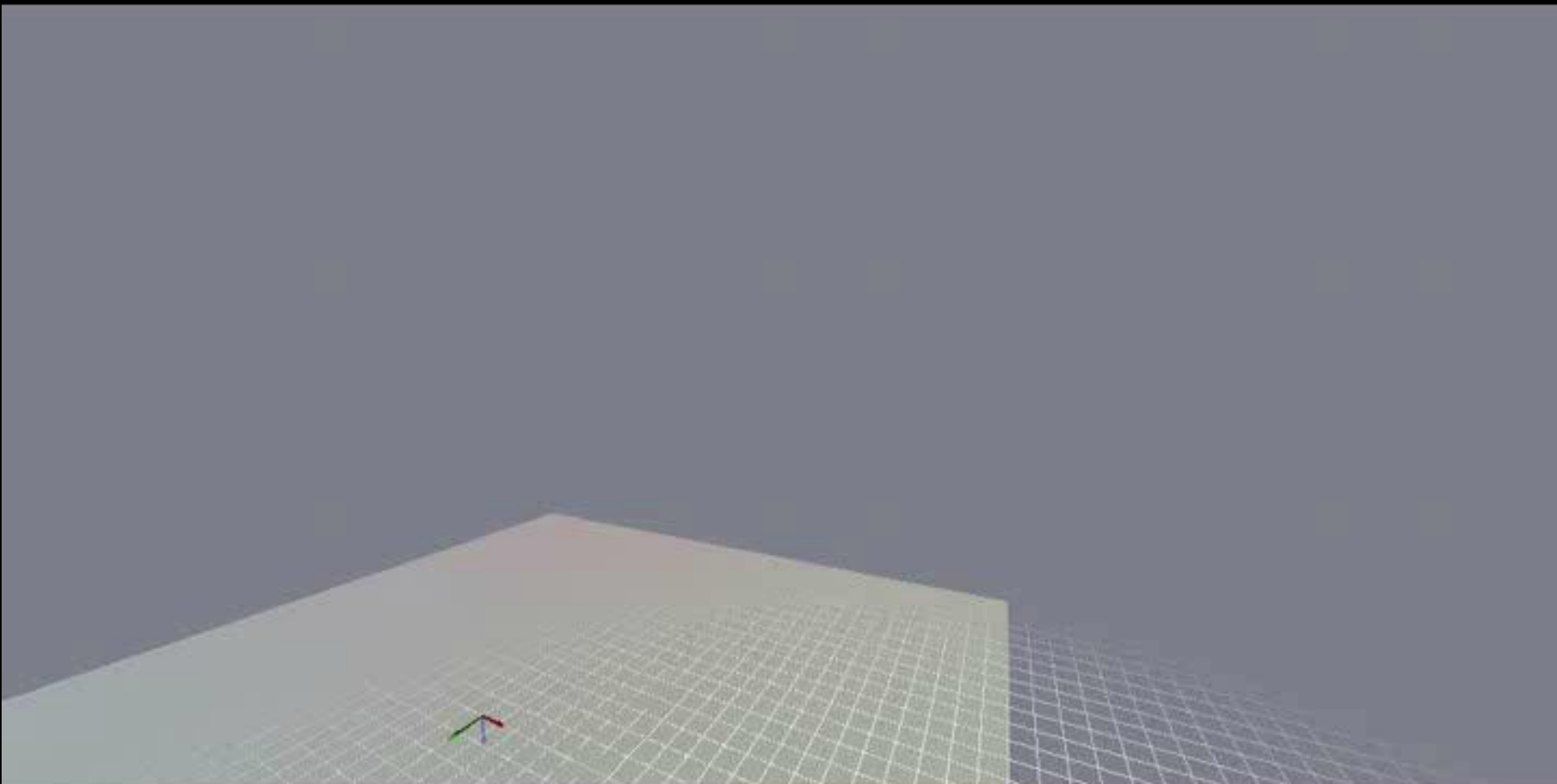
- Expert demonstrates an aerobic sequence several times.
  - Inference algorithm extracts the intended trajectory, and local models used for control.
- We use a receding-horizon DDP controller.
  - Generates a sequence of closed-loop feedback controllers given a trajectory + quadratic penalty.

# Related work

- Bagnell & Schneider, 2001; LaCivita, Papageorgiou, Messner & Kanade, 2002; Ng, Kim, Jordan & Sastry 2004a (2001);
- Roberts, Corke & Buskey, 2003; Saripalli, Montgomery & Sukhatme, 2003; Shim, Chung, Kim & Sastry, 2003; Doherty et al., 2004.
- Gavrillets, Martinos, Mettler and Feron, 2002; Ng et al., 2004b.
- Abbeel, Coates, Quigley and Ng, 2007.
  
- *Maneuvers presented here are significantly **more challenging** and **more diverse** than those performed by any other autonomous helicopter.*

Results: Autonomous airshow

# Results: Flight accuracy



# Conclusion

- Algorithm leverages multiple expert demonstrations to:
  - Infer intended trajectory
  - Learn better models along the trajectory for control.
- First autonomous helicopter to perform extreme aerobatics at the level of an expert human pilot.