

# Learning Influence Probabilities in Social Networks

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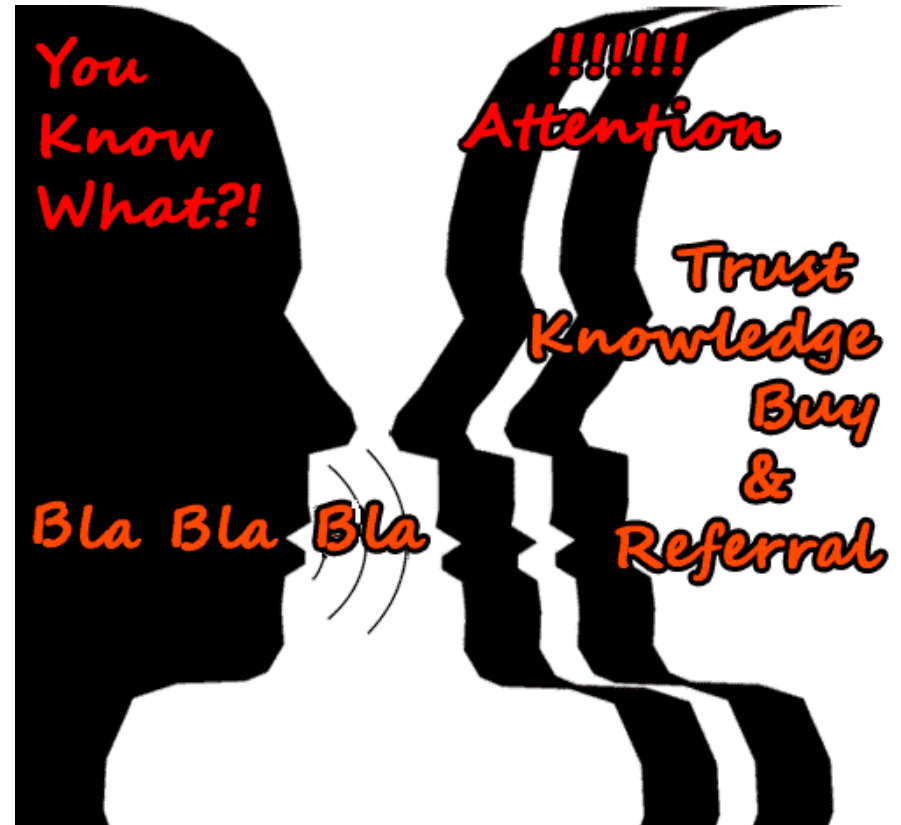


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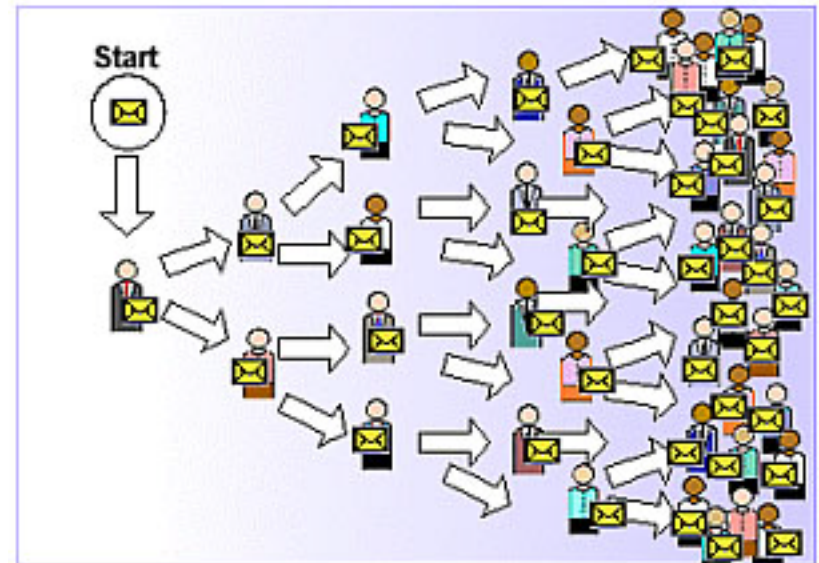
# Word of Mouth and Viral Marketing

- We are more influenced by our friends than strangers
- 68% of consumers consult friends and family before purchasing home electronics (Burke 2003)



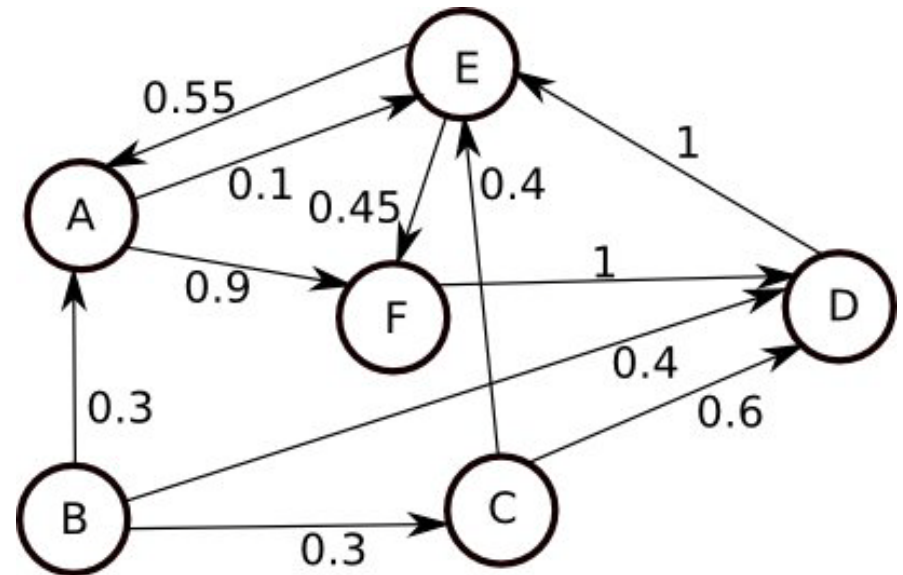
# Viral Marketing

- Also known as Target Advertising
- Initiate chain reaction by Word of mouth effect
- Low investments, maximum gain



# Viral Marketing as an Optimization Problem

- **Given:** Network with influence probabilities
- **Problem:** Select *top-k* users such that by targeting them, the spread of influence is maximized
- *Domingos et al 2001, Richardson et al 2002, Kempe et al 2003*



- **How to calculate true influence probabilities?**

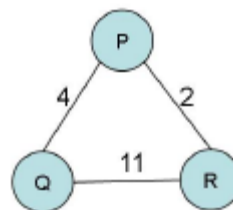
# Some Questions

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- Where do those influence probabilities come from?
  - Available real world datasets don't have prob.!
- Can we learn those probabilities from available data?
- Previous Viral Marketing studies ignore the effect of time.
  - How can we take time into account?
    - Do probabilities change over time?
  - Can we predict time at which user is most likely to perform an action.
- What users/actions are more prone to influence?

# Input Data

- We focus on actions.
- Input:
  - **Social Graph:** P and Q become friends at time 4.
  - **Action log:** User P performs actions a1 at time unit 5.



User	Action	Time
P	a1	5
Q	a1	10
R	a1	15
Q	a2	12
R	a2	14
R	a3	6
P	a3	14

# Our contributions (1/2)

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- Propose several probabilistic influence models between users.
  - Consistent with existing propagation models.
- Develop efficient algorithms to learn the parameters of the models.
- Able to predict whether a user perform an action or not.
- Predict the time at which she will perform it.

# Our Contributions (2/2)

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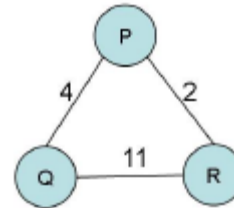
- Introduce metrics of **users and actions influenceability**.
  - High values => genuine influence.
- Validated our models on Flickr.



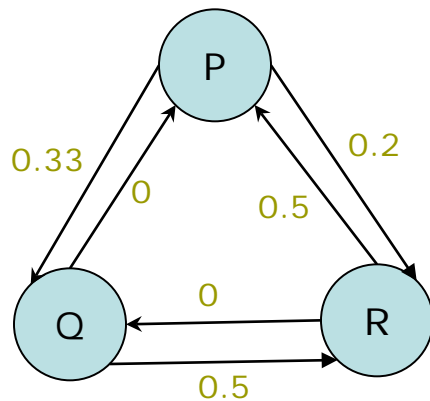
# Overview

## Input:

- **Social Graph:** P and Q become friends at time 4.
- **Action log:** User P performs actions a1 at time unit 5.



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Influence Models



# Background



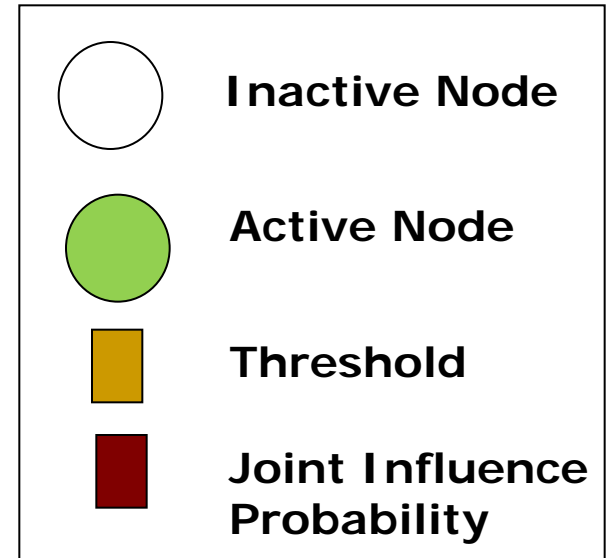
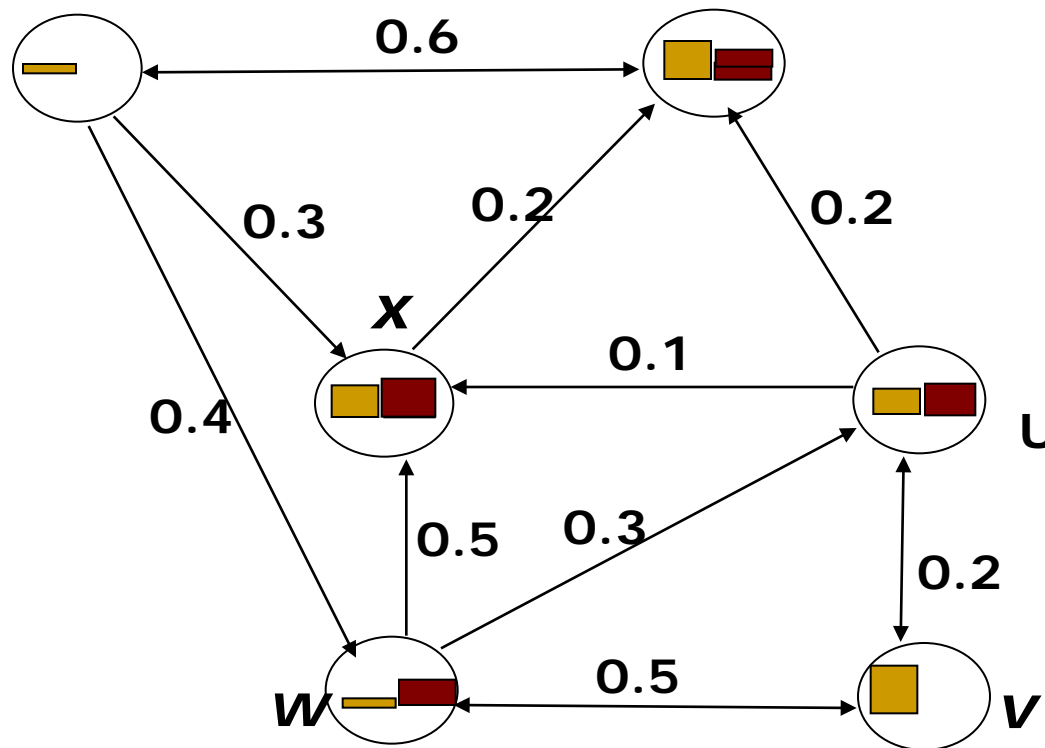
# General Threshold (Propagation)

## Model

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- ❑ At any point of time, each node is either active or inactive.
- ❑ More active neighbors  $\Rightarrow u$  more likely to get active.
- ❑ Notations:
  - $S = \{\text{active neighbors of } u\}$ .
  - $p_u(S)$  : Joint influence probability of  $S$  on  $u$ .
  - $\Theta_u$ : Activation threshold of user  $u$ .
- ❑ When  $p_u(S) \geq \Theta_u$ ,  $u$  becomes active.

# General Threshold Model - Example



***Stop!***

Source: David Kempe's slides

# Our Framework



# Solution Framework

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- Assuming **independence**, we define

$$p_u(S) = 1 - \prod_{v \in S} (1 - p_{v,u})$$

- $p_{v,u}$  : influence probability of user  $v$  on user  $u$
- **Consistent** with the existing propagation models – monotonicity, submodularity.
- It is **incremental**. i.e.  $p_u(S \cup \{w\})$  can be updated incrementally using  $p_u(S)$  and  $p_{w,u}$
  
- Our aim is to learn  $p_{v,u}$  for all edges.

# Influence Models

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## □ Static Models

- Assume that influence probabilities are static and do not change over time.

## □ Continuous Time (CT) Models

- Influence probabilities are continuous functions of time.
- Not incremental, hence very expensive to apply on large datasets.

## □ Discrete Time (DT) Models

- Approximation of CT models.
- Incremental, hence efficient.

# Static Models

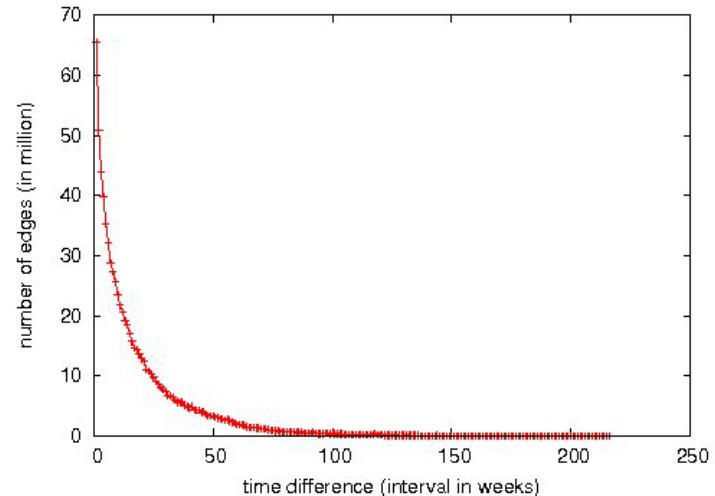
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- 4 variants
  - Bernoulli as running example.
- Incremental hence most efficient.
- We omit details here



# Time Conscious Models

- Do influence probabilities remain constant independently of time?
- We propose **Continuous Time (CT) Model**
  - Based on exponential decay distribution



NO

# Continuous Time Models

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- Best model.
- Capable of **predicting time** at which user is most likely to perform the action.
- Not incremental
  - Discrete Time Model
    - Based on step time functions
    - Incremental

# Evaluation Strategy (1/2)

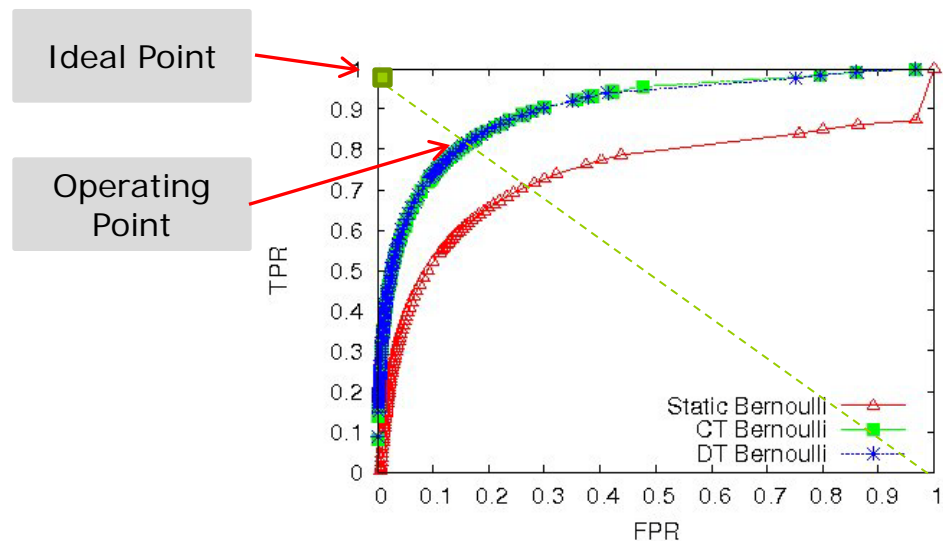
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- Split the action log data into training (80%) and testing (20%).
  - User “James” have joined “Whistler Mountain” community at time 5.
- In testing phase, we ask the model to predict whether user will become active or not
  - Given all the neighbors who are active
  - **Binary Classification**

# Evaluation Strategy (2/2)

- We ignore all the cases when none of the user's friends is active
  - As then the model is inapplicable.
- We use **ROC** (Receiver Operating Characteristics) curves
  - True Positive Rate (TPR) vs False Positive Rate (FPR).
  - $TPR = TP/P$
  - $FPR = FP/N$

	Reality		
		Active	Inactive
Prediction	Active	TP	FP
	Inactive	FN	TN
	Total	P	N



# Algorithms

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- Special emphasis on efficiency of applying/testing the models.
  - Incremental Property
  
- In practice, action logs tend to be huge, so we optimize our algorithms to minimize the number of scans over the action log.
  - Training: 2 scans to learn all models simultaneously.
  - Testing: 1 scan to test one model at a time.

# Experimental Evaluation

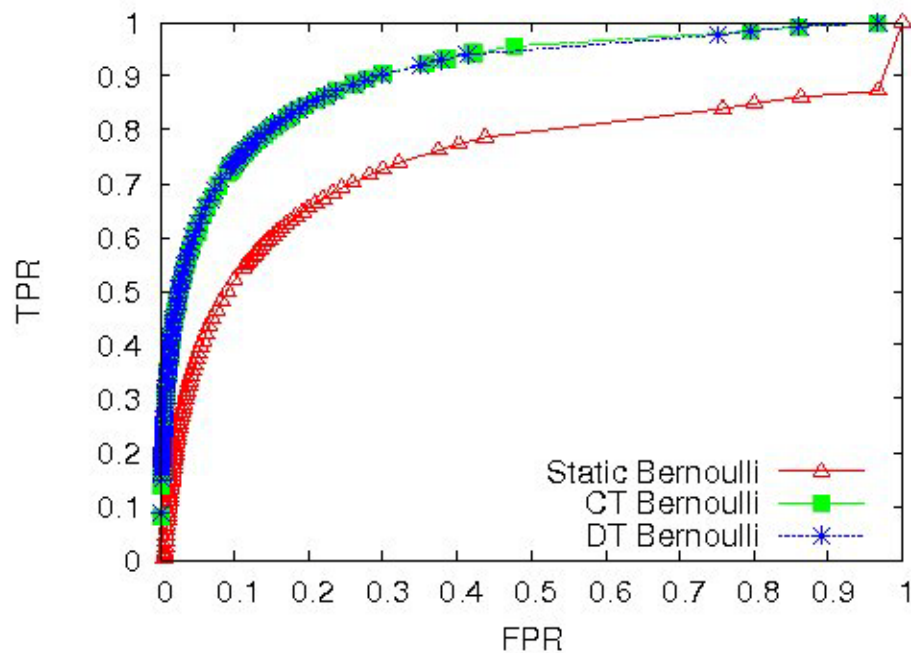


# Dataset

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- Yahoo! Flickr dataset
- “Joining a group” is considered as action
  - User “James” joined “Whistler Mountains” at time 5.
- #users ~ 1.3 million
- #edges ~ 40.4 million
- Degree: 61.31
- #groups/actions ~ 300K
- #tuples in action log ~ 35.8 million

# Comparison of Static, CT and DT models

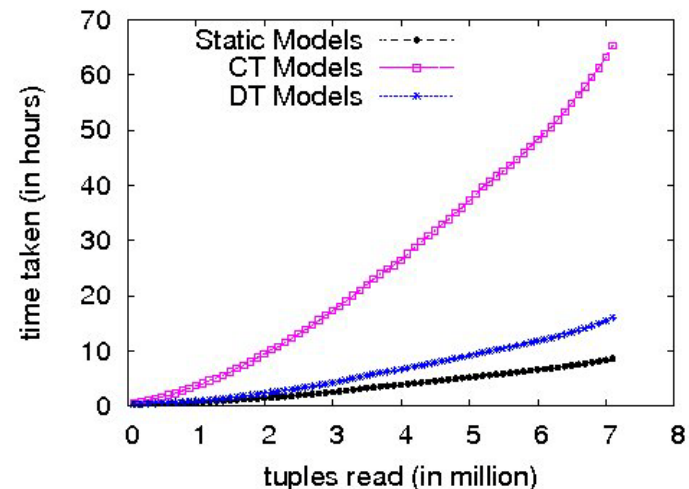


- ❑ Time conscious Models are better than Static Models.
- ❑ CT and DT models perform equally well.



# Runtime

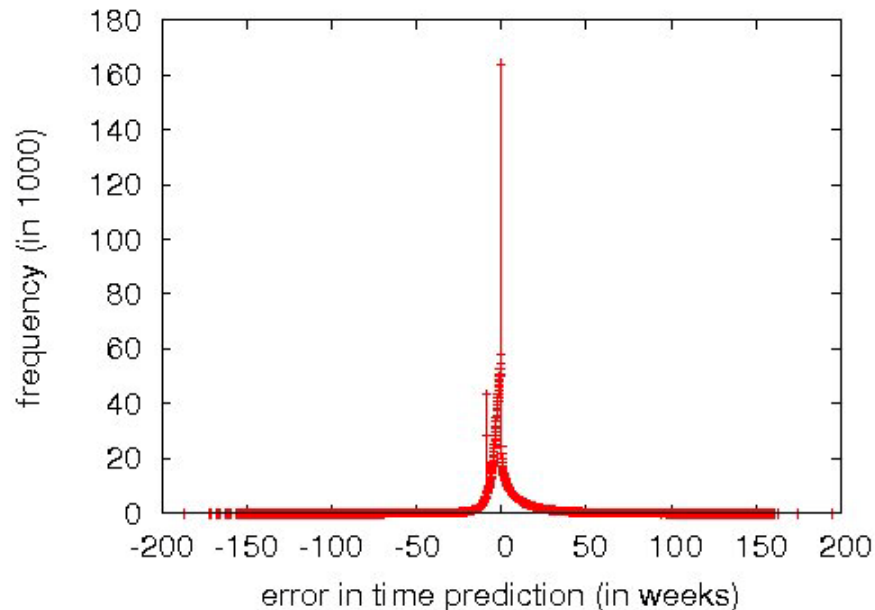
## Testing



- Static and DT models are far more efficient compared to CT models because of their **incremental** nature.

# Predicting Time – Distribution of Error

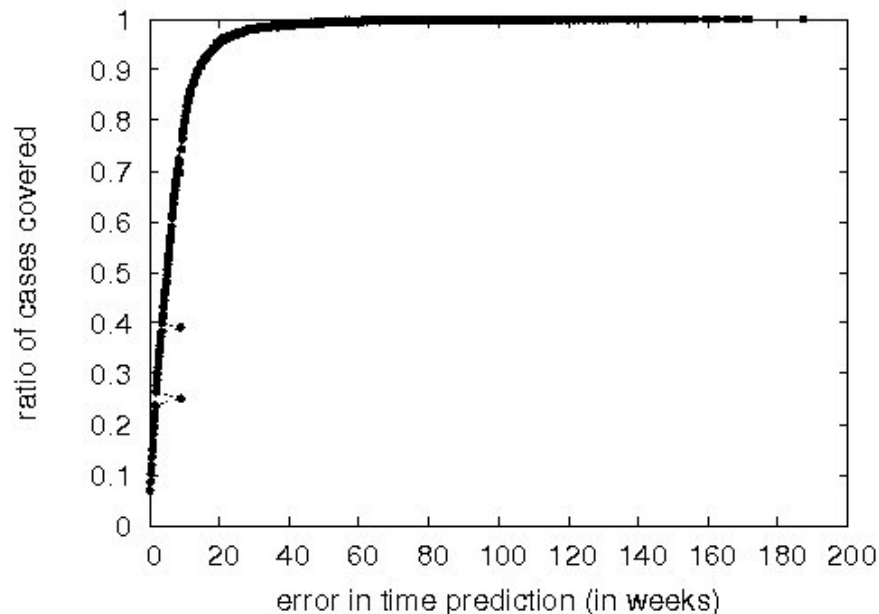
- Operating Point is chosen corresponding to
  - TPR: 82.5%, FPR: 17.5%.



- X-axis: error in predicting time (in weeks)
- Y-axis: frequency of that error
- Most of the time, error in the prediction is very small

# Predicting Time – Coverage vs Error

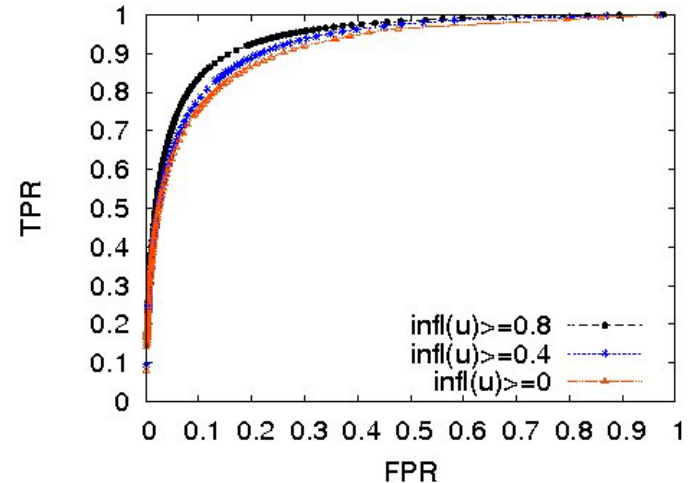
- Operating Point is chosen corresponding to
  - TPR: 82.5%, FPR: 17.5%.



- A point  $(x,y)$  here means for  $y\%$  of cases, the error is within  $\pm x$
- In particular, for 95% of the cases, the error is within 20 weeks.

# User Influenceability

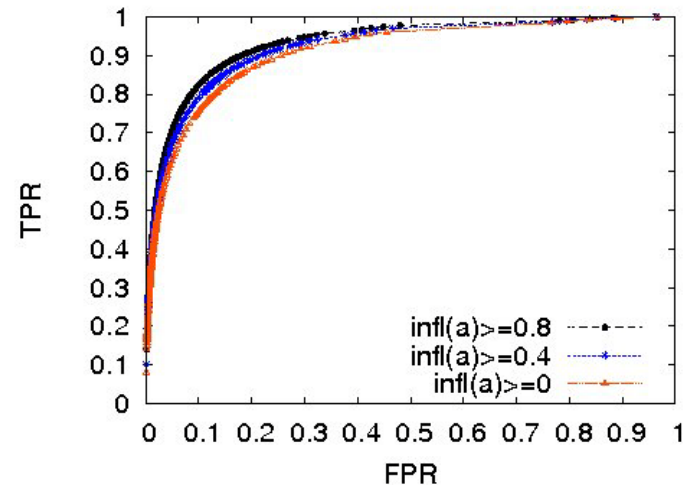
- Some users are more prone to influence propagation than others.
- Learn from Training data



- Users with high influenceability => easier prediction of influence => more prone to viral marketing campaigns.

# Action Influenceability

- Some actions are more prone to influence propagation than others.



- Actions with high user influenceability => easier prediction of influence => more suitable to viral marketing campaigns.

# Related Work

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- Independently, Saito et al (KES 2008) have studied the same problem
  - Focus on Independent Cascade Model of propagation.
  - Apply Expectation Maximization (EM) algorithm.
  - Not scalable to huge datasets like the one we are dealing in this work.

# Other applications of Influence Propagations

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- Personalized Recommender Systems
  - Song et al 2006, 2007
- Feed Ranking
  - Samper et al 2006
- Trust Propagation
  - Guha et al 2004, Ziegler et al 2005, Golbeck et al 2006, Taherian et al 2008

# Conclusions (1/2)

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- ❑ Previous works typically assume influence probabilities are given as input.
- ❑ Studied the problem of learning such probabilities from a log of past propagations.
- ❑ Proposed both static and time-conscious models of influence.
- ❑ We also proposed efficient algorithms to learn and apply the models.



# Conclusions (2/2)

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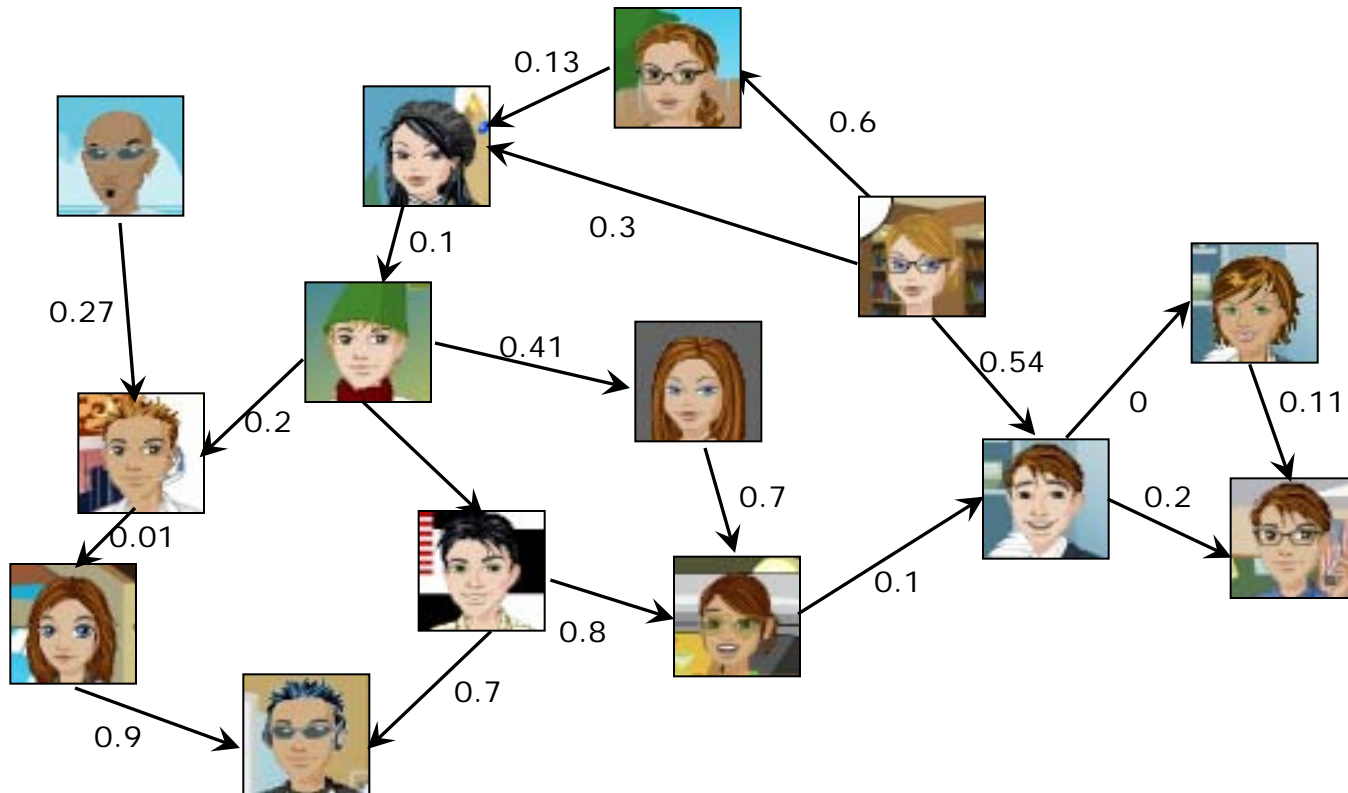
- Using CT models, it is possible to predict even the time at which a user will perform it with a good accuracy.
- Introduce metrics of users and actions influenceability.
  - High values => easier prediction of influence.
  - Can be utilized in Viral Marketing decisions.

# Future Work

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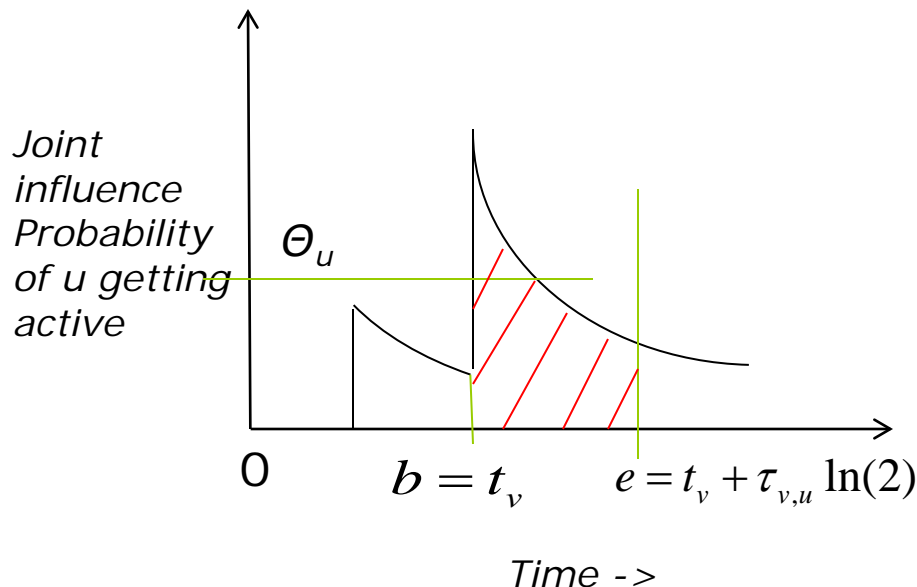
- Learning optimal user activation thresholds.
- Considering users and actions influenceability in the theory of Viral Marketing.
- Role of time in Viral Marketing.

# Thanks!!



# Predicting Time

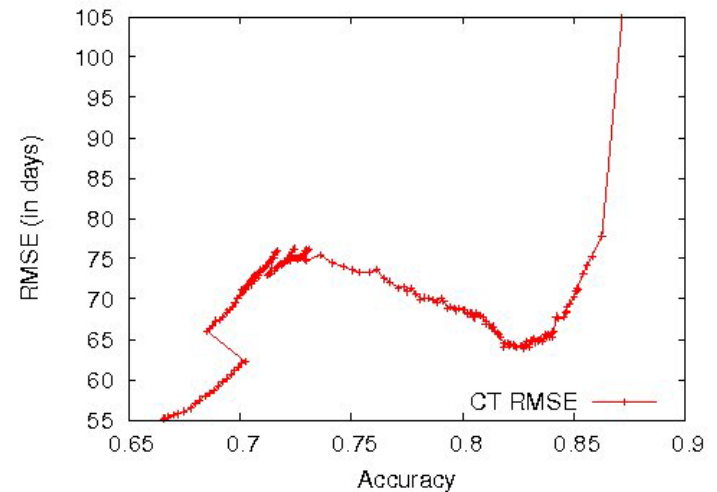
- CT models can predict the time interval  $[b, e]$  in which she is most likely to perform the action.



- $\tau_{v,u} \ln(2)$  is half life period
- Tightness of lower bounds not critical in Viral Marketing Applications.
- Experiments on the upper bound  $e$ .

# Predicting Time - RMSE vs Accuracy

- CT models can predict the time interval [b,e] in which user is most likely to perform the action.
  - Experiments only on upper bound e.
- Accuracy =  $\frac{\text{\# cases when the prediction of upper bound is correct}}{\text{\# total cases}}$
- RMSE = root mean square error
- RMSE ~ 70-80 days



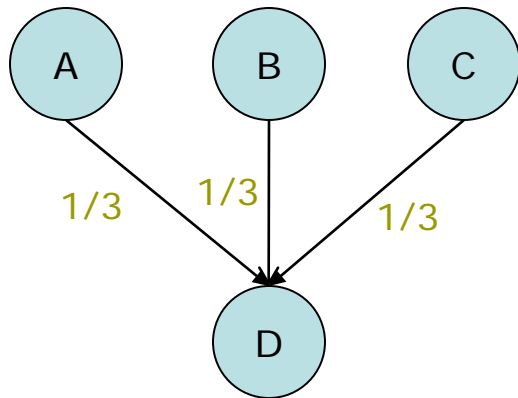
# Static Models – Jaccard Index

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- Jaccard Index is often used to measure similarity b/w sample sets.
- We adapt it to estimate  $p_{v,u}$

$$p_{v,u} = \frac{\text{\# of actions propagated from v to u}}{\text{\# of actions performed by v or u}}$$

# Partial Credits (PC)



- Let, for an action, D is influenced by 3 of its neighbors.
- Then,  $1/3$  credit is given to each one of these neighbors.

PC Bernoulli  $\longrightarrow$   $p_{v,u} = \frac{\text{total credits accumulated}}{\text{total number of actions } v \text{ performed}}$

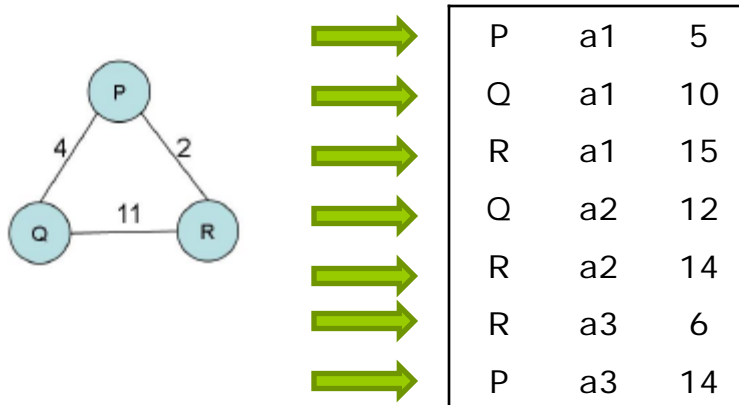
PC Jaccard  $\longrightarrow$   $p_{v,u} = \frac{\text{total credits accumulated}}{\text{total number of actions } v \text{ or } u \text{ performed}}$

# Learning the Models

## Parameters to learn:

- #actions performed by each user –  $A_u$
- #actions propagated via each edge –  $A_{v2u}$
- Mean life time –  $\tau_{v,u}$

u	$A_u$
P	0
Q	0
R	0



	P	Q	R
P	X	0,0	<del>10,10</del>
Q	0,0	X	0,0
R	0,0	0,0	X

$A_{v,u}, \tau_{v,u}$



# Propagation Models

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- Threshold Models
  - Linear Threshold Model
  - General Threshold Model
  
- Cascade Models
  - Independent Cascade Model
  - Decreasing Cascade Model

# Properties of Diffusion Models

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## □ Monotonicity

$$p_u(S) \leq p_u(T) \text{ whenever } S \subseteq T$$

## □ Submodularity – Law of marginal Gain

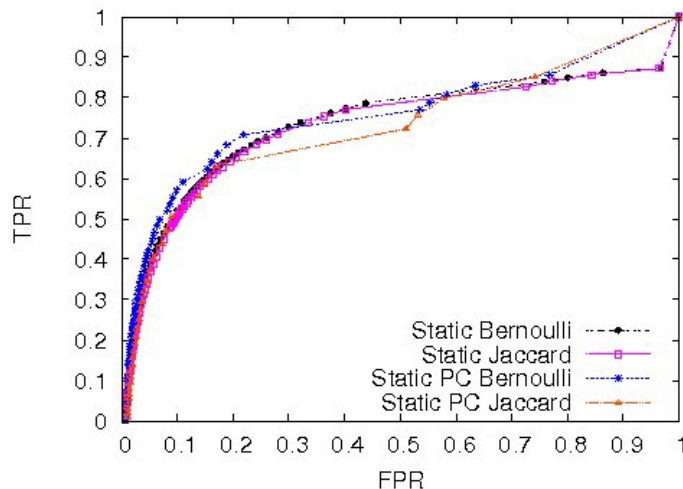
$$p_u(S \cup \{w\}) - p_u(S) \geq p_u(T \cup \{w\}) - p_u(T)$$

whenever  $S \subseteq T$

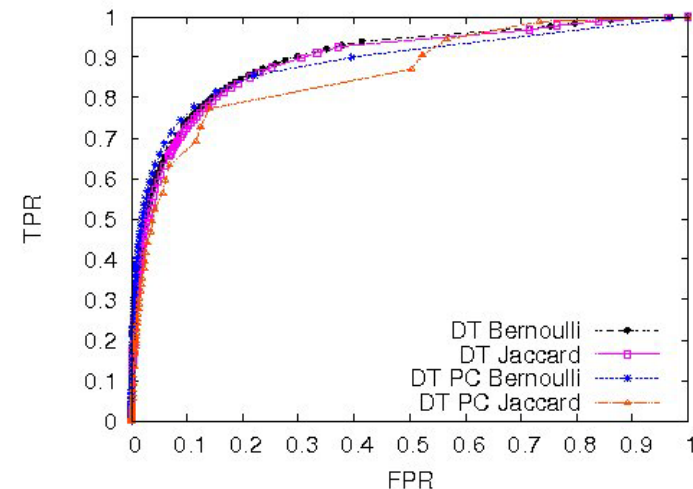
## □ Incrementality (Optional)

$p_u(S \cup \{w\})$  can be updated incrementally  
using  $p_u(S)$  and  $p_{w,u}$

# Comparison of 4 variants



ROC comparison of 4 variants of **Static Models**

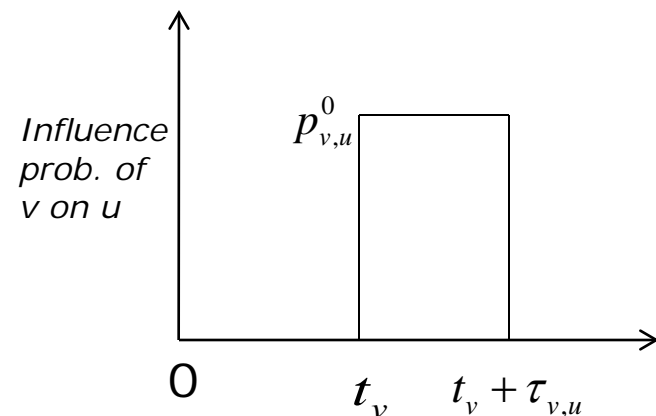
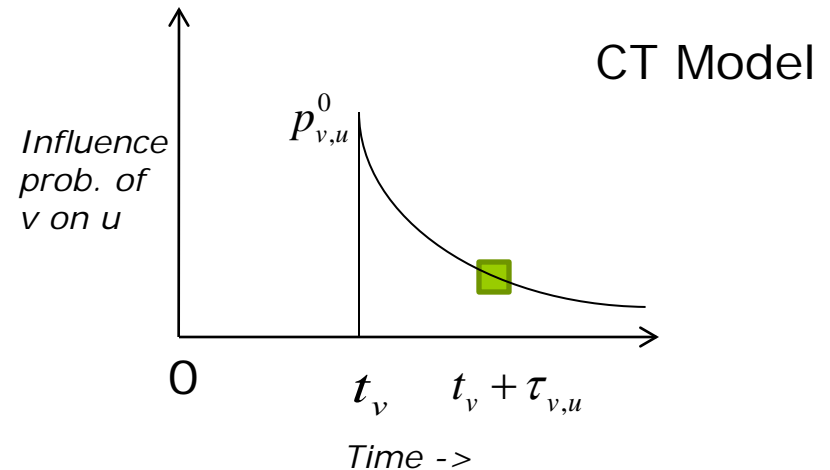


ROC comparison of 4 variants of **Discrete Time (DT) Models**

- Bernoulli is slightly better than Jaccard
- Among two Bernoulli variants, Partial Credits (PC) wins by a small margin.

# Discrete Time Models

- Approximation of CT Models
- Incremental, hence efficient
- 4-variants corresponding to 4 Static Models



DT Model

# Overview

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- Context and Motivation
- Background
- Our Framework
- Algorithms
- Experiments
- Related Work
- Conclusions

# Continuous Time Models

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## □ Joint influence probability

$$p_u^t(S) = 1 - \prod_{v \in S} (1 - p_{v,u}^t)$$

## □ Individual probabilities – exponential decay

$$p_{v,u}^t = p_{v,u}^0 e^{-(t-t_u)/\tau_{v,u}}$$

- $p_{v,u}^0$  : maximum influence probability of  $v$  on  $u$
- $\tau_{v,u}$  : the mean life time.

# Algorithms

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- **Training** – All models simultaneously in no more than 2 scans of training sub-set (80% of total) of action log table.
- **Testing** – One model requires only one scan of testing sub-set (20% of total) of action log table.
- Due to the lack of time, we omit the details of the algorithms.