

Minimax Localization of Structural Information in Large Noisy Matrices

Poster: W055

M. Kolar



S. Balakrishnan

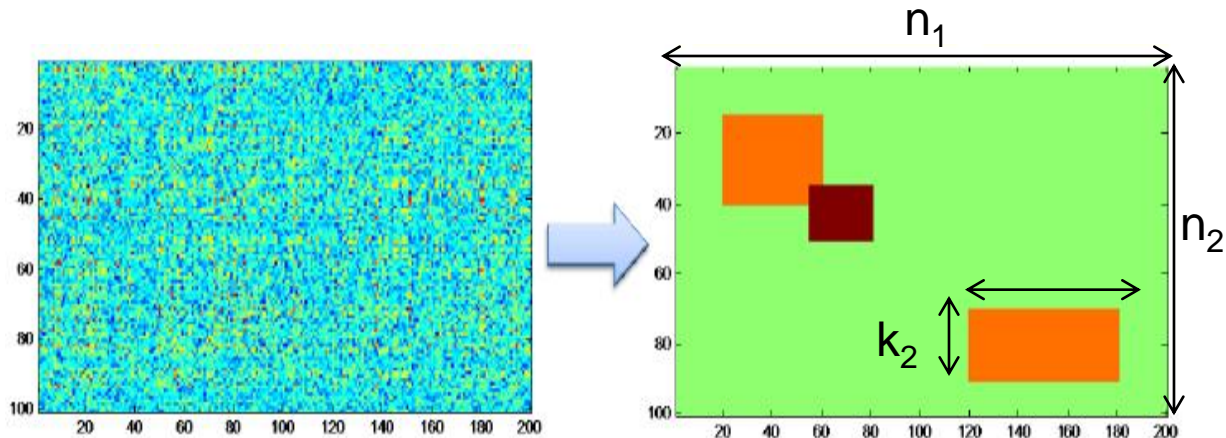


A. Rinaldo



A. Singh

Identifying biclusters



Goal: De-noise and re-order rows/columns of the matrix to infer biclusters that are activated.

Observation model

$$\mathbf{A} = \beta \mathbf{u}\mathbf{v}^T + \mathbf{R}$$

\mathbf{u} – k_1 sparse unit vector
 \mathbf{v} – k_2 sparse unit vector
 $\mathbf{u}, \mathbf{v} \propto \{-1, 0, 1\}$

$\mathbf{R} \sim$ i.i.d. zero-mean subgaussian(σ^2) perturbation

Identifying biclusters

Information Theoretic minimax limit: If

$$\text{SNR} \quad \frac{\beta}{\sigma} \sim \sqrt{\frac{k_1 k_2 \log(n_1 n_2)}{\min(k_1, k_2)}}$$

then, for **any** biclustering procedure, the probability of failure remains bounded away from zero by a constant.

Note:

Optimal performance achieved by scanning over all submatrices of size $k_1 \times k_2$.

Computationally efficient procedures

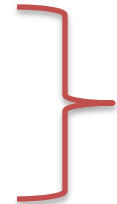
SNR

Elementwise thresholding

Sparse Singular Value Decomposition

Row/Column Averaging

(large clusters only $k \sim n^{1/2+\alpha}$)


$$\frac{\beta}{\sigma} \sim \sqrt{k_1 k_2 \log(n_1 n_2)}$$

$$\frac{\beta}{\sigma} \sim \frac{\sqrt{k_1 k_2 \log(n_1 n_2)}}{\min(n_1^\alpha, n_2^\alpha)}$$

Note:

These procedures do not achieve information theoretic lower bound.