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# Fast and Memory-Efficient Discovery of the Top-k Relevant Subgroups in a Reduced Candidate Space

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# Introduction

## Subgroup Discovery and the Theory of Relevance

# The Task of Subgroup Discovery

Input:

- examples, characterized by features
- a target class

Output:

- top- $k$  subgroup descriptions
  - subgroup that are **large** and have a **high target share**

$$\text{e.g. } \text{quality}(sd) = n_{sd} \cdot (p_{sd} - p_0)$$

- Subgroup description = conjunction of features

Example:

<b>Approval</b>	Children = yes	Children = no	University	High Income
+		+	+	+
+	+		+	+
+	+			
-		+		+
-	+			
-	+			
-		+		

# The Task of Subgroup Discovery

Input:

- examples, characterized by features
- a target class

Output:

- top-k subgroup descriptions

1.	High_Inc & University
2.	University
3.	High_Inc
4.	High_Inc & Univ & Children=no
5.	High_Inc & Univ & Children=yes
...	
8.	Children=yes

1. and 2. are equivalent

4. and 5. are irrelevant given 1.

Approval	Children = yes	Children = no	University	High Income
+		+	+	+
+	+		+	+
+	+			
-		+		+
-	+			
-	+			
-		+		

# The Theory of Relevance

Def: **Relevance** [Lavrac et al, JLP-99]

- A subgroup is **irrelevant** if it is dominated
- $s$  is **dominated** by  $t$  in DB iff.
  - $TP(DB,s) \subseteq TP(DB,t)$
  - $FP(DB,s) \supseteq FP(DB,t)$

Example:

“**HighInc&Univ&Child=no**”  
is dominated by  
“**HighInc&Univ**”

<b>Approval</b>	Children = yes	Children = no	University	High Income
+		+	+	+
+	+		+	+
+	+			
-		+		+
-	+			
-	+			
-		+		

# Relevant top- $k$ Subgroup Discovery

Lavrac & Gamberger: Relevancy in constraint-based subgroup discovery, 2005

Input:

- a set of examples characterized by features
- a target class

Output:

- the  $k$  highest-quality *relevant* subgroup descriptions

Description	Classic sd	Closed sd	Relevant sd
High_Inc & University	1 <sup>st</sup>	1 <sup>st</sup>	1 <sup>st</sup>
University	2 <sup>nd</sup>		
High_Inc	3 <sup>rd</sup>	2 <sup>nd</sup>	
Children=yes & High_Inc & University	4 <sup>th</sup>	3 <sup>rd</sup>	
Children=yes & High_Inc	5 <sup>th</sup>		
Children=no & High_Inc & University	6 <sup>th</sup>	4 <sup>th</sup>	
Children=no & High_Inc	7 <sup>th</sup>		
Children=yes	8 <sup>th</sup>	5 <sup>th</sup>	2 <sup>nd</sup>

# Existing Approaches

... and their limitations

# Pruning-based Approaches to Relevant SD

e.g. Lemmerich & Atzmueller: Fast discovery of relevant subgroup patterns, FLAIRS 2010

Idea:

- Traverse the space of subgroup descriptions, e.g. using DFS
  - Keep track of the  $k$  best subgroup visited
- Apply pruning
  - Use quality of the  $k$ -best subgroup (" $\theta_k$ ") as minimum quality threshold
  - Prune branches whose quality can be derived to be below  $\theta_k$
- **Local relevance check**
  - Whenever a new high-quality subgroup is visited, check dominance between the  $k+1$  best subgroups

→ Output consists of relevant subgroups





# Approach based on the Closed-on-the-positives

Garriga et al.: Closed sets for labeled data, JML-08

- Proposition: A subgroup description  $sd$  is relevant iff.
  - It is **closed on the positives**
  - There is no cpos generalization  $s_g \subseteq sd$  with same support in the negatives
- Approach:
  - Collect all closed-on-the-positives
  - Remove irrelevant subgroups in a post-processing step
- **Advantages: exact**  
# cpos can be exponentially smaller than # closed / all sd
- **Problems: huge memory requirements; no pruning**

# Summary of the existing Approaches

- Pruning-based approach:
  - doesn't guarantee exact results
  
- C-pos approach:
  - infeasible for large number of c-pos
  - no pruning

# A new Approach

... based on iterative deepening and an efficient relevance check

# Efficient relevant subgroup discovery

An efficient algorithm should

1. only consider the *closed-on-the-positive* subgroups
2. avoid high memory requirements
3. apply pruning based on  $\theta_k$ 
  - Requires an exact relevance check at visiting time

# An $O(k)$ Relevance Check

## **Proposition:**

For many popular quality functions\*, relevance of a closed-on-the-positive  $sd$  can be checked based only the **higher-quality** relevant generalizations

$$G^* = \{s_g \subseteq sd \mid s_g \text{ is relevant and has } \mathbf{higher\ quality} \text{ than } sd\}$$

## **Hence:**

If we are only interested in relevance of **subgroups with quality  $> \theta_k$** , and we visit the **cpos** in a **general-to-specific** fashion

then relevance can be checked using **only the top-k subgroups visited**

→ Memory requirements:  $k$  subgroups, instead of  $O(2^{\text{length}(sd)})$

\* : in particular, for  $q(sd) = n^a (p-p_0)$ , with  $0 \leq a \leq 1$

# The New Algorithm ID-Rsd

## Idea

- Perform an iterative deepening
- Only keep track of the best  $k$  subgroups visited
- Perform relevance check by comparing with the  $k$  best subgroups

## Properties:

- *Exact solution*
- *Memory requirements:  $O(k)$  subgroups (+ Iterative deepening DFS)*
- *Max. number of nodes visited is  $O(|\mathcal{C}_p| \cdot n)$ , where  $n \sim$  number of features*
- *Allows pruning based on  $\theta_k$*

Depending on shape  
of search space

# Comparison with existing Approaches

Algorithm	Memory	Runtime	Pruning
Classic SD	$O(n^2 + kn)$	$O( S  n m)$	Yes
Closed SD	$O(n^2 + kn)$	$O( C  n^2 m)$	Yes
RelSD_Classic	No exact result, otherwise like above		
RelSD_Cpos	$\Omega( C_p  n)$	$\Omega( C_p  n^2 m)$	No
ID-Rsd	$O(n^2 + kn)$	$O( C_p  (n^3 m + n^2 k))$	Yes

$S$  ~ Subgroups (all) +  
 $C$  ~ Closed subgroups  
 $C_p$  ~ Closed on the positives

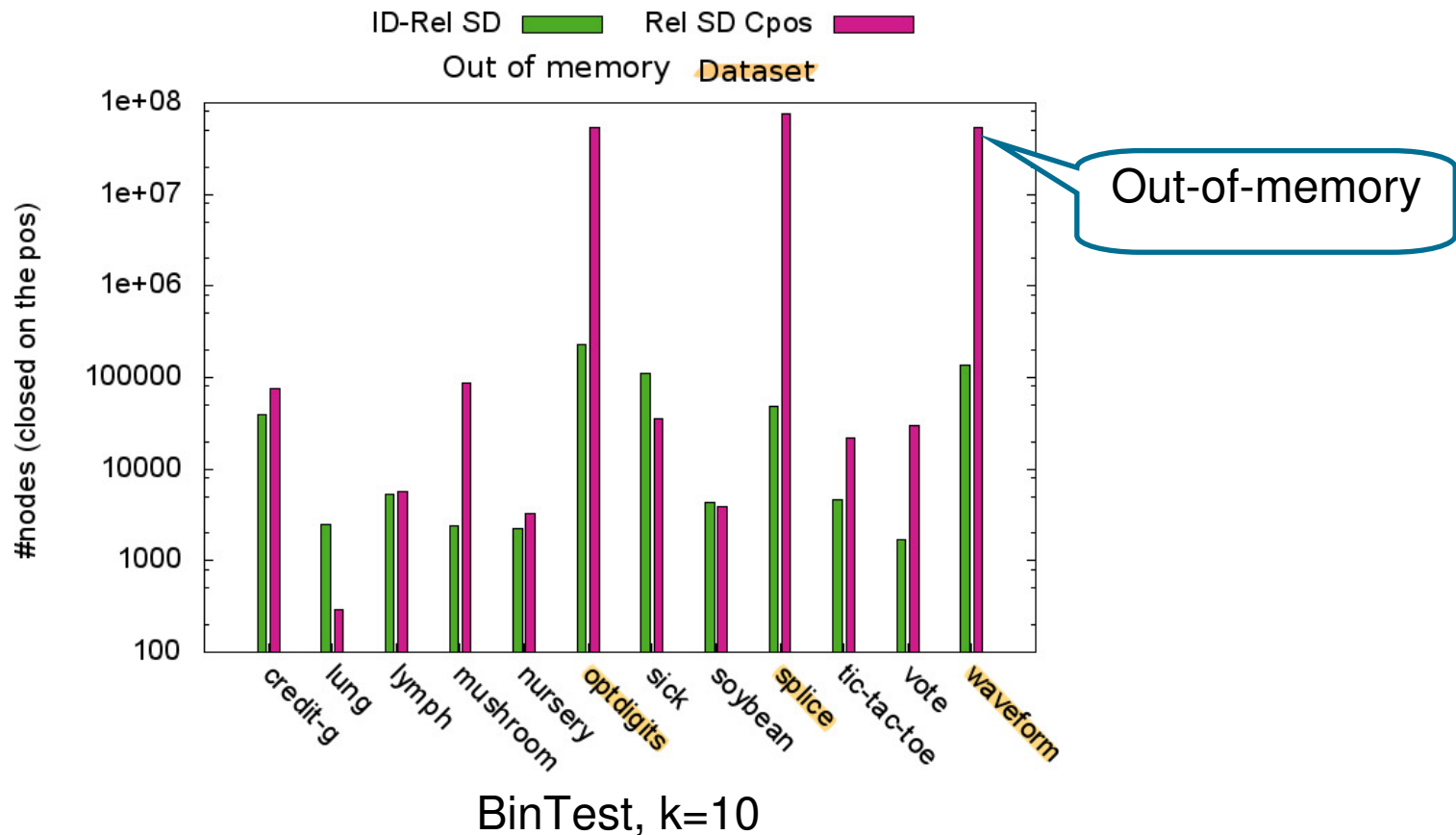
No worse than classic/closed

$n$  ~ # features  
 $m$  ~ # records



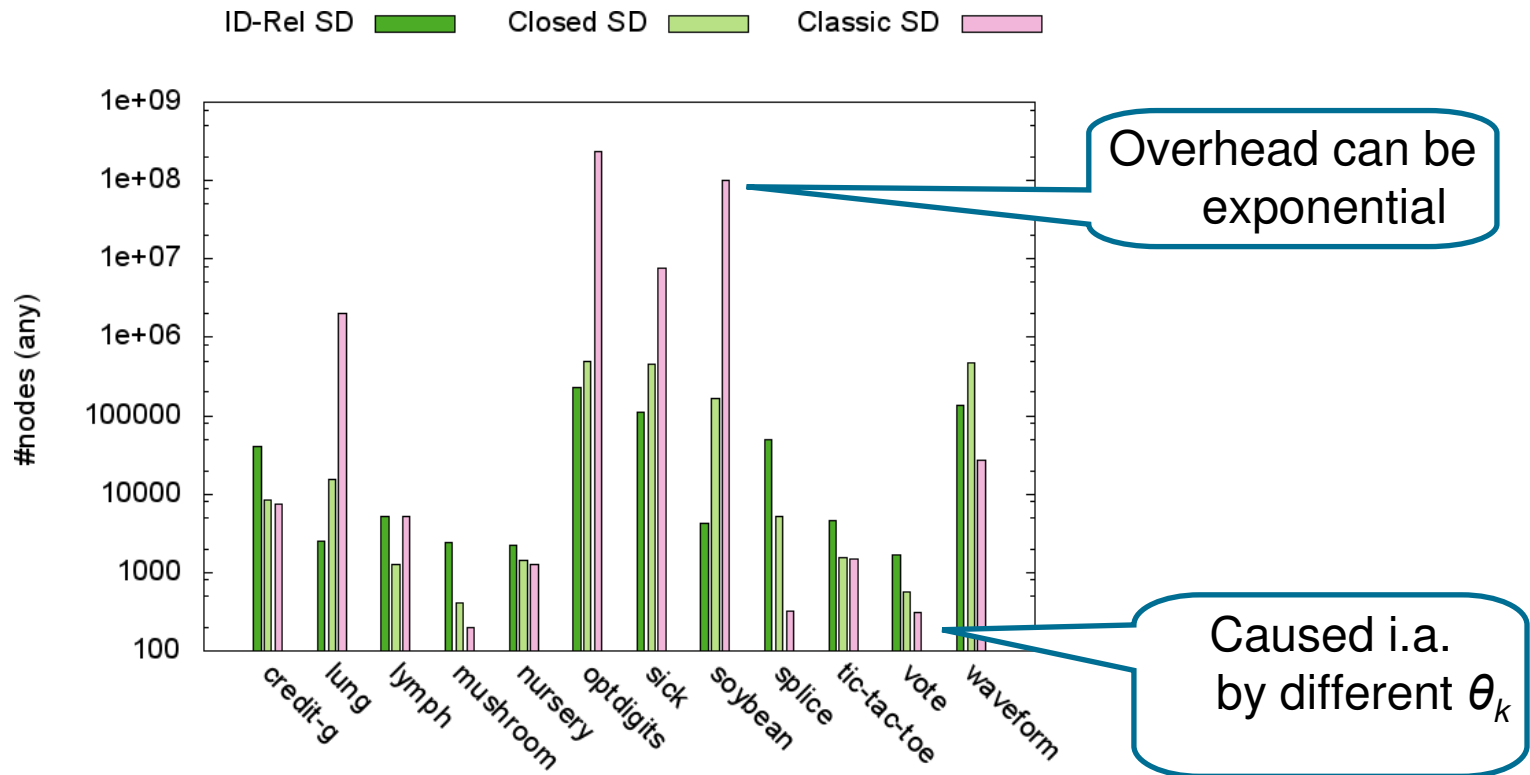
# Empirical Evaluation

# Comparison with the Closed-on-the-positives Approach



Overall: lower memory requirements, lower number of nodes & much faster

# Comparison with Classic & Closed SD Approaches



	ID-Rsd	ClassicSD	ClosedSD	Cpos-Rsd
Total runtime	118 sec	2717 sec	286 sec	?

# Summary

# Summary

- Relevant SD yields more valuable patterns than classic SD
- ID-Rsd
  - First exact Rsd approach with polynomial memory requirements
  - Much faster than C-pos approach
  - Competitive with exhaustive classic/closed SD approaches

*Thank you very much for your attention!*