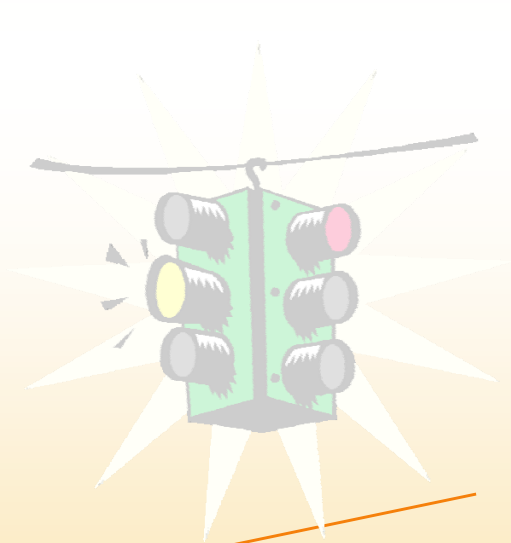




A METHOD FOR DEVELOPING PRELIMINARY FRICTION DETERIORATION MODEL ON RUNWAY

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Introduction

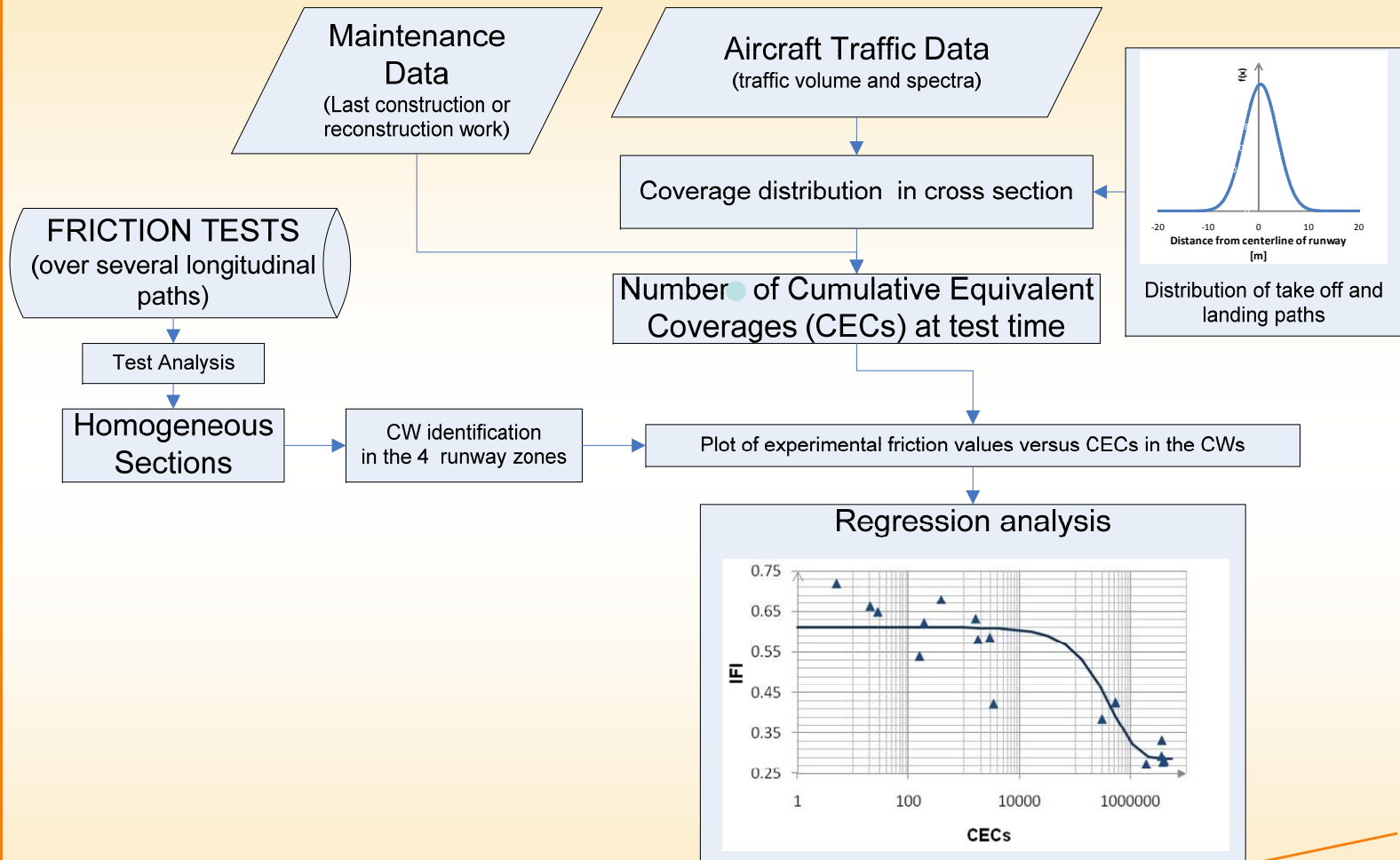
The aim of this paper is, on one side, to set up a deteriorating model of friction, by analyzing lateral variability of a runway in a regional airport;

On the other side, to give a contribution to develop common measurement procedure.

Framework

- **Cumulative number of equivalent coverages (CECs) in the runway cross section points is calculated from input data (annual aircraft movements, traffic spectra, construction time and aircraft path distribution);**
- **Friction tests are run along several longitudinal paths in a single test session;**
- **Experimental results of friction tests are analysed for localizing homogeneous sections;**

- Runway is divided in 4 zone, bearing the landing phases in mind and to look at the mean friction value of the homogeneous sections (zone 1 *touchdown*, zone 2 *aircraft deceleration by ground spoiler and thrust reversers*, zone 3 *aircraft deceleration by wheel brakes* and zone 4 *approach to exit*);
- A critical window (CW) containing only homogeneous sections (i.e. inside which there are not section border) and the lowest IFI values are identified in the four runway zones;
- Friction values in the CW are plotted versus CECs;
- Regression analysis is run for fitting deterioration model to experimental data.



Equivalent Coverages

Coverages (R) are numbers of times that a point on a runway is expected to be stressed by a wheel;

Equivalency Factor take into account the different damages produced by several aircraft types and gears

$$EC = R * EF$$

$$R_{nose}(x, y) = \begin{cases} \lnw_{nose} & \text{if } y \in \left\{ \left[-\frac{i_{nose}}{2} - \frac{a_{nose}}{2} + x; -\frac{i_{nose}}{2} + \frac{a_{nose}}{2} + x \right] \cup \left[\frac{i_{nose}}{2} - \frac{a_{nose}}{2} + x; \frac{i_{nose}}{2} + \frac{a_{nose}}{2} + x \right] \right\} \\ 0 & \text{elsewhere} \end{cases}$$

$$R_{main_left}(x, y) = \begin{cases} \lnw_{main} & \text{if } y \in \left\{ \left[-\frac{i_{nose}}{2} - \frac{a_{nose}}{2} - d + x; -\frac{i_{nose}}{2} + \frac{a_{nose}}{2} - d + x \right] \cup \left[\frac{i_{nose}}{2} - \frac{a_{nose}}{2} - d + x; \frac{i_{nose}}{2} + \frac{a_{nose}}{2} - d + x \right] \right\} \\ 0 & \text{elsewhere} \end{cases}$$

$$R_{main_right}(x, y) = \begin{cases} \lnw_{main} & \text{if } y \in \left\{ \left[-\frac{i_{nose}}{2} - \frac{a_{nose}}{2} + d + x; -\frac{i_{nose}}{2} + \frac{a_{nose}}{2} + d + x \right] \cup \left[\frac{i_{nose}}{2} - \frac{a_{nose}}{2} + d + x; \frac{i_{nose}}{2} + \frac{a_{nose}}{2} + d + x \right] \right\} \\ 0 & \text{elsewhere} \end{cases}$$

\lnw_{main} is the number of wheels along longitudinal direction of main landing gear (1, 2 or 3);

\lnw_{nose} is the number of wheels along longitudinal direction of nose landing gear;

X is the distance of aircraft longitudinal axel from the runway centreline;

y is the distance of the surface point from the runway centreline;

i_{nose} is distance between nose landing gear wheels;

a_{nose} is diameter of nose landing gear wheel contact area;

i_{main} is distance between wheels of each main landing gear;

a_{main} is diameter of main landing gear wheel contact area;

d is distance between main landing gears.

$$R_{i_take-off}(x, y) = R_{nose_take-off}(x, y) + R_{main_left_take-off}(x, y) + R_{main_right_take-off}(x, y)$$

$$R_{i_landing}(x, y) = R_{nose_landing}(x, y) + R_{main_left_landing}(x, y) + R_{main_right_landing}(x, y)$$

$$PR_{i_take-off}(y) = \int_{-\infty}^{+\infty} f_{take-off}(x) \cdot R_{i_take-off}(x, y) dx$$

$$PR_{i_landing}(y) = \int_{-\infty}^{+\infty} f_{landing}(x) \cdot R_{i_landing}(x, y) dx$$

$$N_{i_dec}(y) = n_{i_dec} \cdot PR_{i_dec}(y)$$

$$N_{i_landing}(y) = n_{i_landing} \cdot PR_{i_landing}(y)$$

$$N_{tot_take-off}(y) = \sum_i N_{i_take-off}(y)$$

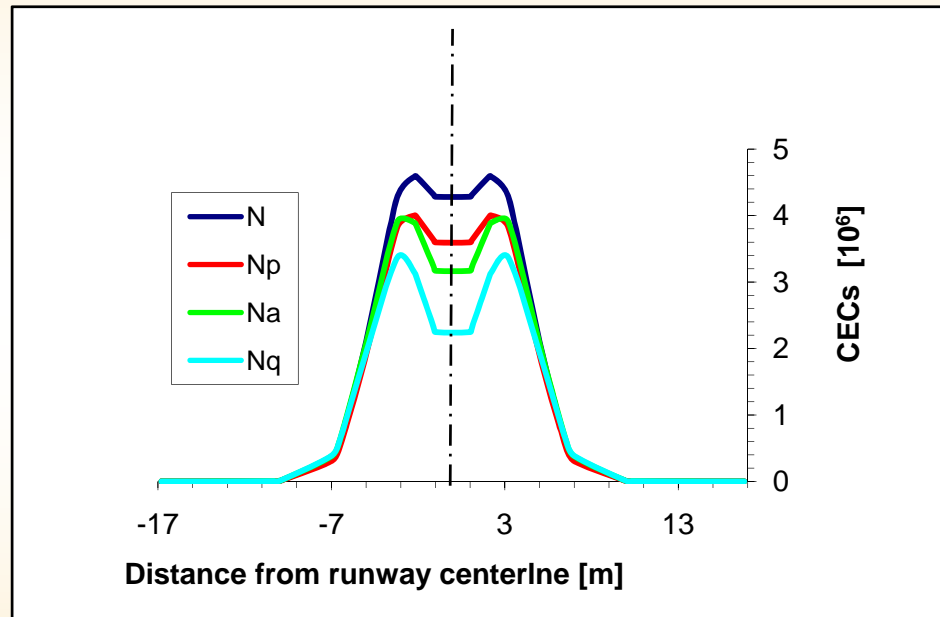
$$N_{tot_landing}(y) = \sum_i N_{i_landing}(y)$$

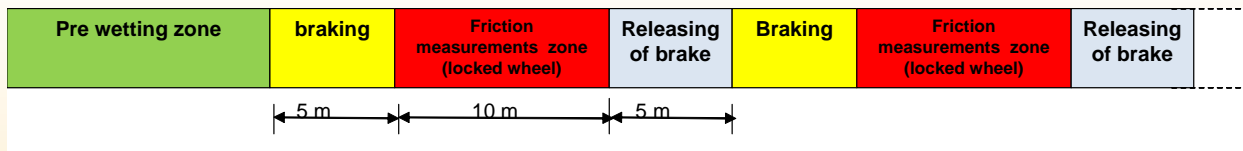
$$N_{TOT}(y) = N_{tot_landing}(y) + N_{tot_take-off}(y)$$

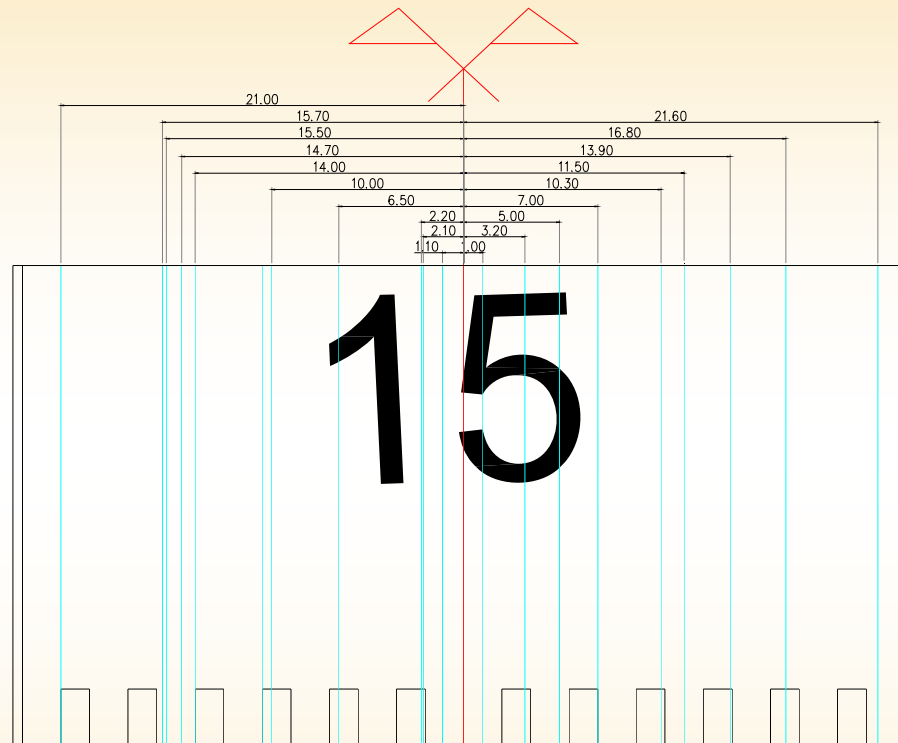
$$k_{i,j}^P = \frac{P_{i,j}}{P_{rv,rw}}$$

$$k_{i,j}^A = \frac{A_{i,j}}{A_{rv,rw}}$$

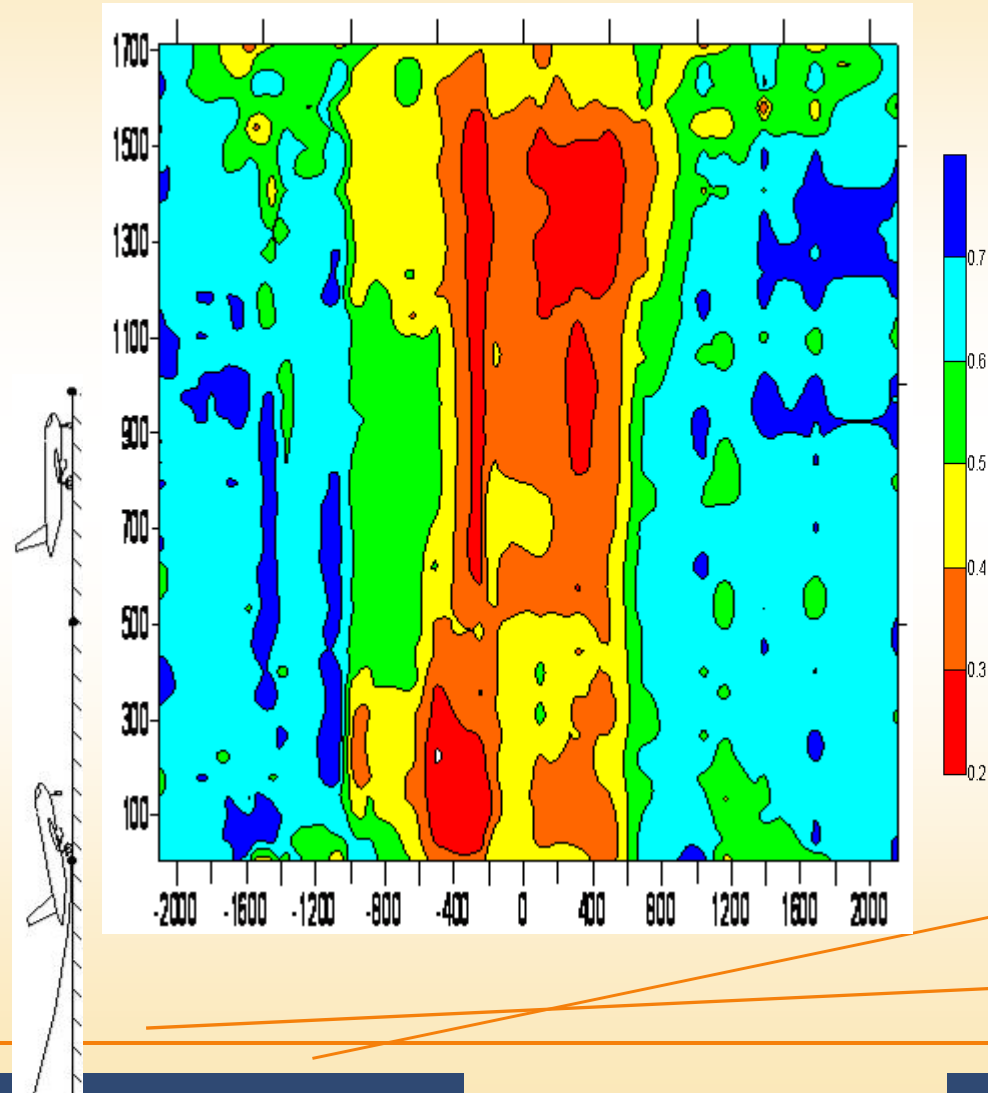
$$k_{i,j}^L = \frac{L_{i,j}}{L_{rv,rw}}$$







Distances from the runway centerline [m]																			
-21	-15.7	-15.5	-14.7	-14	-10.5	-10	-6.5	-2.2	-2.1	-1.1	1	3.2	5	7	10.3	11.5	13.9	16.8	21.6



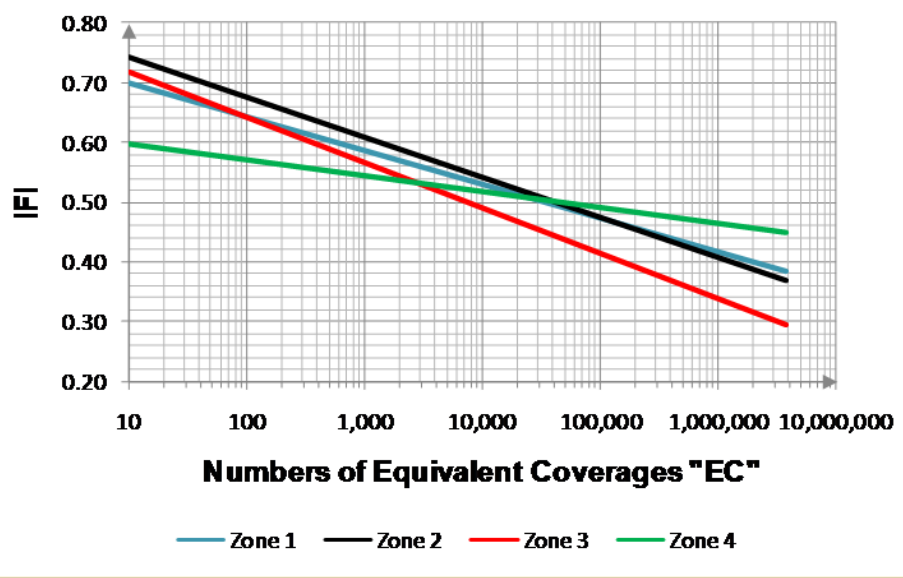
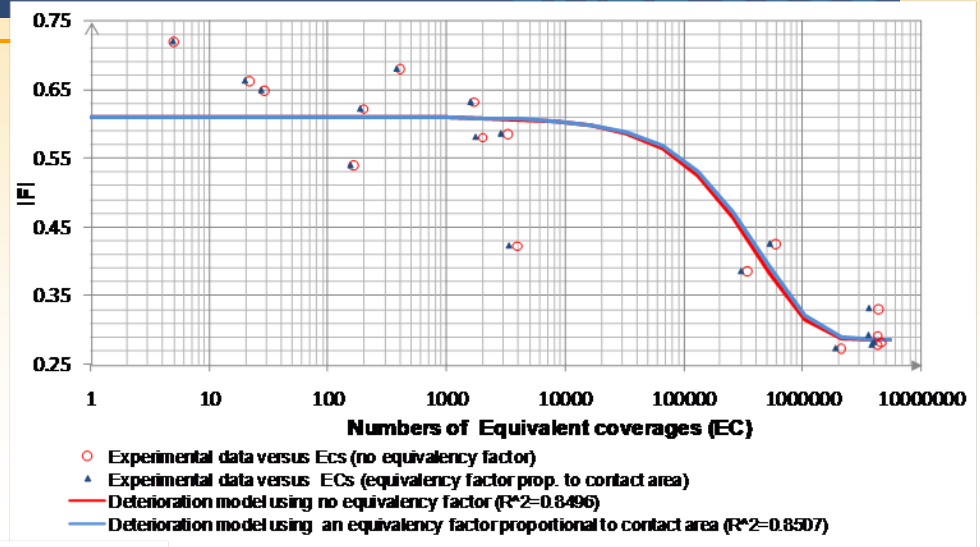
	Description	Distance from touch down marking of beginning and end of zone	Distance from touch down marking of beginning and end of CCS
Zone 1	touchdown	From 0 m to 300 m	From 105 m to 145 m
Zone 2	aircraft deceleration by ground spoiler and thrust reversers	From 300 m to 1200 m	From 985 m to 1025 m
Zone 3	aircraft deceleration by wheel brakes	From 1200 m to 1500 m	From 1385 m to 1465 m
Zone 4	approach to exit	From 1500 m to 1750 m	From 1585 m to 1700 m

Y (m)	X (m)																															
	0	20	40	60	80	100	120	140	160	180	200	220	240	260	280	300	320	340	360	380												
1705	0.638																															
1696	0.693										0.692																					
1686	0.693					0.663															0.524											
1676	0.664					0.663					0.723					0.549										0.477		0.593				
1666	0.699			0.645				0.747												0.661			0.540									
1656	0.644							0.686					0.622										0.567									
1646	0.596				0.699												0.665										0.581					
1636	0.529		0.462				0.525					0.594										0.423			0.585							
1626	0.432					0.531										0.527					0.467			0.426				0.521				
1616	0.301					0.390					0.308										0.249					0.369						
1606	0.320			0.356					0.435					0.348					0.283					0.354			0.436					
1596	0.456					0.383															0.332					0.463						
1586	0.391			0.493					0.383			0.449		0.358					0.293					0.408								
1576	0.375					0.422					0.318					0.276			0.300			0.279					0.441					
1566	0.360		0.440		0.386					0.406			0.339					0.274					0.460									
1556	0.620												0.534					0.366			0.518											
1546	0.659										0.676					0.586																
1536	0.545		0.527		0.695										0.632					0.530												
1526	0.574			0.675												0.729		0.641		0.660					0.575							
1516	0.667							0.567			0.677					0.731		0.597		0.720					0.567							
1506	0.671				0.616		0.666										0.716			0.665												

$$IFI(EC) = a \cdot \text{Log}(EC) + b$$

$$IFI(EC) = a \cdot e^{-b \cdot (EC)} + c$$

ZONE	parameter	No equivalence factor		CEF proportional to contact area		CEF proportional to tyre pressure		CEF proportional to wheel load	
		logarithm model	shifted exponential model	logarithm model	shifted exponential model	logarithm model	shifted exponential model	logarithm model	shifted exponential model
VALUES OF THE MODEL PARAMETERS									
1	a	-0.055	0.2559	-0.056	0.264	-0.055	0.256	-0.057	0.299
	b	0.752	-1.20E-06	0.755	-9.81E-07	0.752	-1.33E-06	0.757	-7.23E-07
	c	-	0.3630	-	0.354	-	0.362	-	0.319
2	a	-0.065	0.3353	-0.066	0.347	-0.066	0.336	-0.067	0.376
	b	0.806	-1.06E-06	0.808	-9.08E-07	0.805	-1.16E-06	0.809	-7.97E-07
	c	-	0.3205	-	0.309	-	0.319	-	0.280
3	a	-0.073	0.3230	-0.075	0.324	-0.074	0.323	-0.076	0.326
	b	0.785	-2.29E-06	0.790	-2.12E-06	0.784	-2.56E-06	0.793	-2.03E-06
	c	-	0.2869	-	0.286	-	0.287	-	0.284
4	a	-0.026	0.1480	-0.026	0.162	-0.026	0.150	-0.026	0.175
	b	0.624	-6.97E-07	0.624	-5.74E-07	0.623	-7.53E-07	0.624	-5.81E-07
	c	-	0.4162	-	0.402	-	0.414	-	0.389
SUM OF SQUARE OF THE RESIDUALS (SSR)									
1		0.0750	0.0762	0.0762	0.0757	0.0747	0.0760	0.0775	0.0732
2		0.0792	0.0174	0.0837	0.0167	0.0786	0.0173	0.0879	0.0152
3		0.0479	0.0714	0.0482	0.0709	0.0481	0.0715	0.0490	0.0703
4		0.0274	0.0109	0.0288	0.0108	0.0272	0.0109	0.0300	0.0108
COEFFICIENT OF DETERMINATION (R ²)									
1		0.7613	0.7574	0.7574	0.7589	0.7621	0.7580	0.7532	0.7671
2		0.8110	0.9583	0.8001	0.9601	0.8123	0.9586	0.7901	0.9638
3		0.8991	0.8496	0.8985	0.8507	0.8987	0.8493	0.8969	0.8519
4		0.6653	0.8661	0.6482	0.8683	0.6669	0.8664	0.6334	0.8677



CONCLUSIONS

Experimental survey allowed us to map friction on runway;

The minimum value of friction was localized in the second half of the runway (700 to 1400 m), at a distance from centerline between 2 and 4 m, where the coverages are maximum!!

Furthermore models, constructed using statistical regression, fit well experimental data, and the Independent Variable "Equivalent Coverage" seems to represent quite well actions of several aircraft types.